

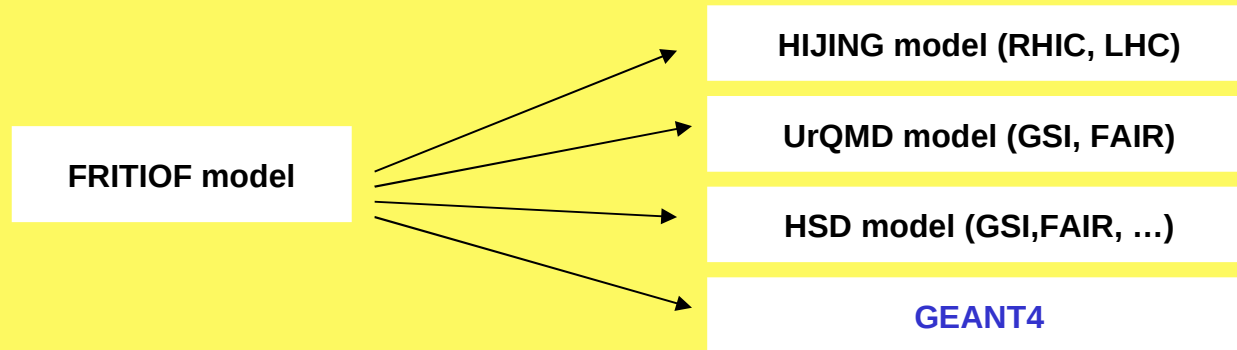
Development of the Fritiof Model in Geant4

Vladimir Uzhinsky, (On behalf of the Geant4 Hadronics Working Group)
MC-2010. Tokyo, Japan

B. Andersson et al., Nucl. Phys. $\{\bf B281\}$ (1987) 289;

B. Nilsson-Almqvist and E. Stenlund, Comp. Phys. Commun. 43 (1987) 387.

The well established Fritiof model is in the core of modern MC codes:
HIJING, UrQMD, HSD, ART. Now it is adapted in Geant4 also!



Our aim – extension of Geant4 string models to low energy domain

Content

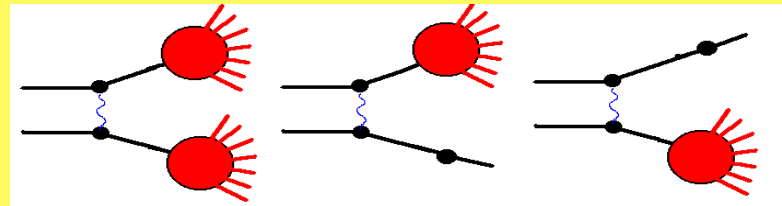
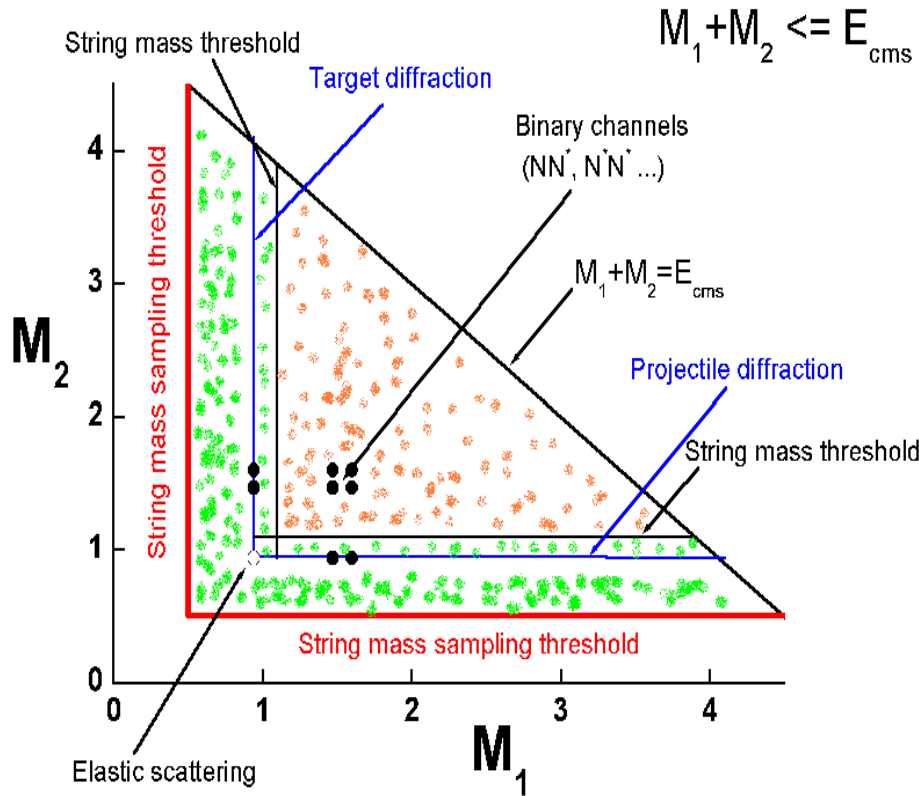
1. Short description of the models;
2. Separate simulation of diffraction dissociation;
3. Simulation of binary reactions and low mass string frag.;
4. Correction of multiplicity of intra-nuclear collisions;
5. Fit of RTIM parameters;
6. Results;
7. Conclusion

1. FRITIOF model

It is assumed binary kinematics of hadron-hadron interactions

$$a + b \rightarrow a' + b', \quad m_{a'} > m_a \quad m_{b'} > m_b$$

where a' и b' are excited states of initial hadrons a and b .



$$dW \propto \frac{dM_1}{M_1}, \quad dW \propto \frac{dM_2}{M_2}$$

$$M_{\text{string}} = 1.1 \text{ GeV (N)}, 1 \text{ GeV } (\pi), 1.1 \text{ GeV (K)}$$

$$M_{\text{sampling}} = 0.94 \text{ GeV (N)}, 0.75 \text{ GeV } (\pi), 0.85 \text{ GeV (K)}$$

$$dW \propto dP_{\text{proj}}^- / P_{\text{proj}}^-$$

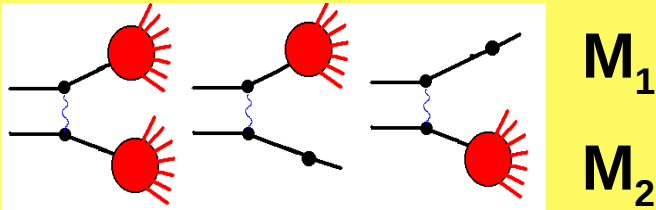
$$dW \propto dP_{\text{tar}}^+ / P_{\text{tar}}^+$$

In hadron-nucleus interactions the excited hadrons can interact with other nucleons of nucleus and increases mass. The probability of multiple collisions is calculated in Glauber approach. The used variant of model Fritiof is enlarged with elastic re-scatterings of hadrons. The excited states are considered as QCD-strings and LUND model are used for their fragmentation.

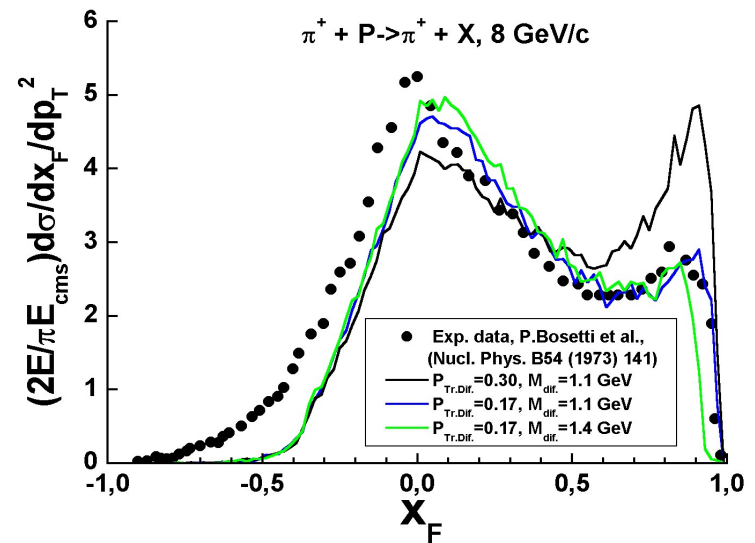
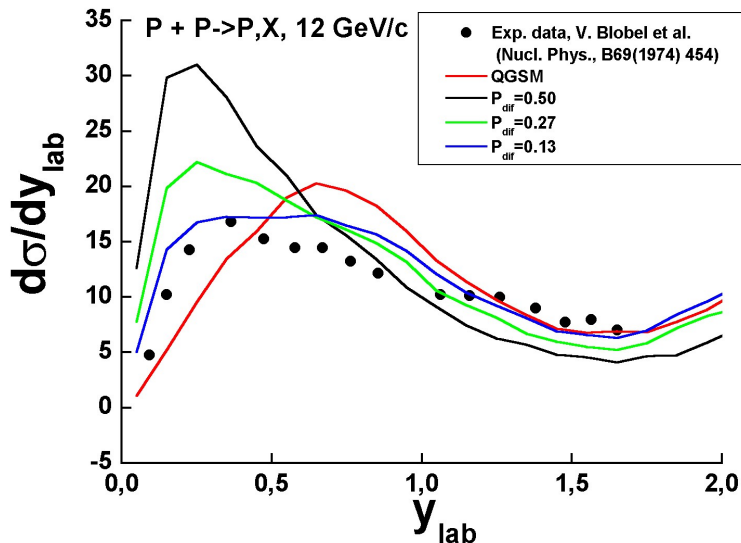
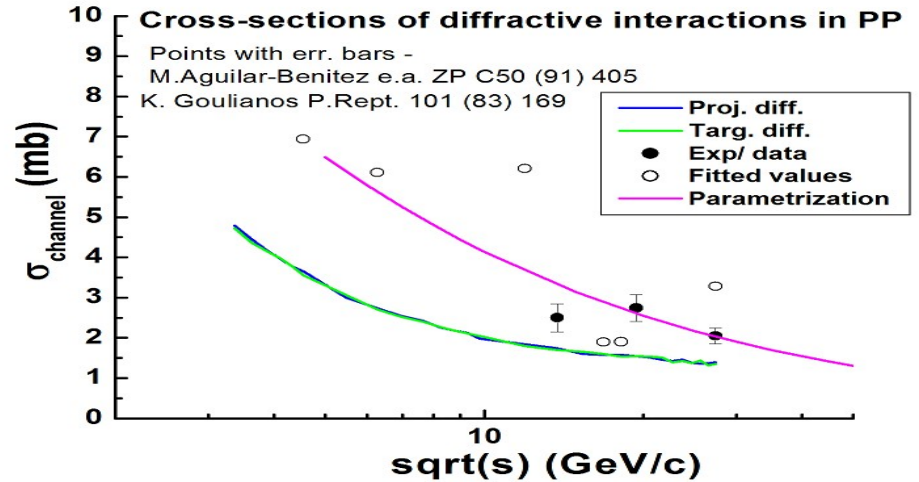
2. Separate simulation of diffraction dissociation

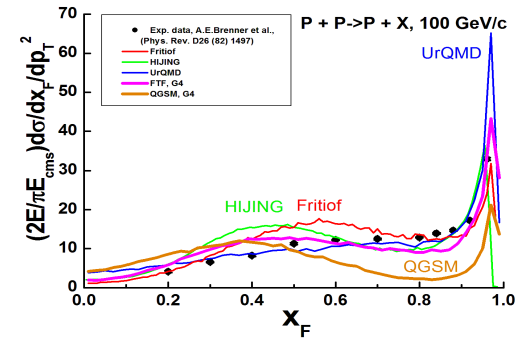
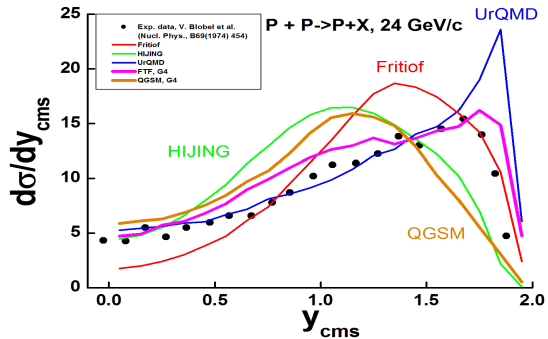
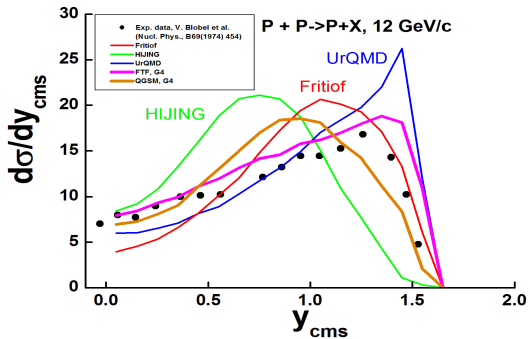
3

We simulate separately diffractive and non-diffractive interactions.



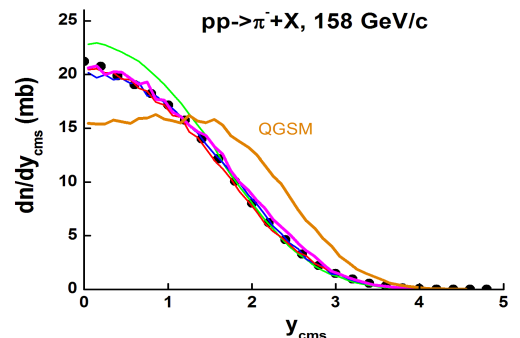
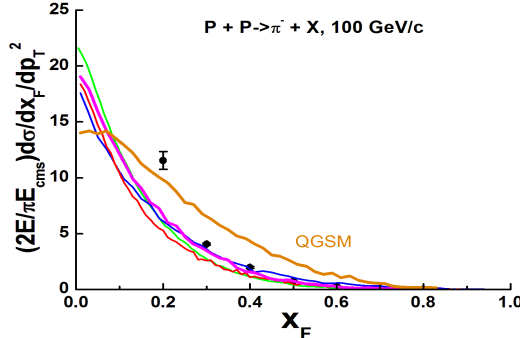
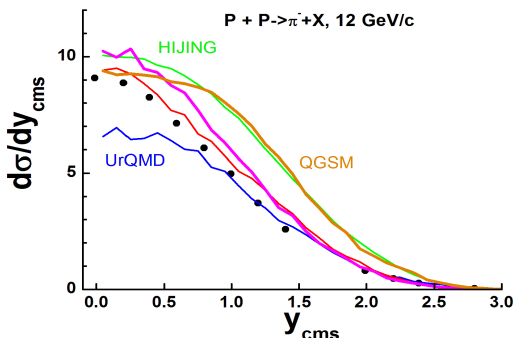
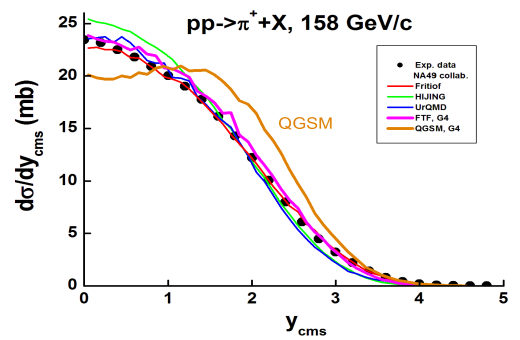
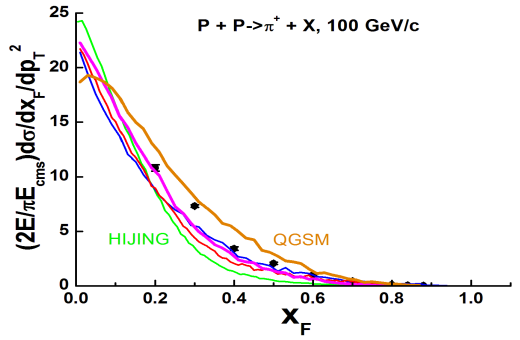
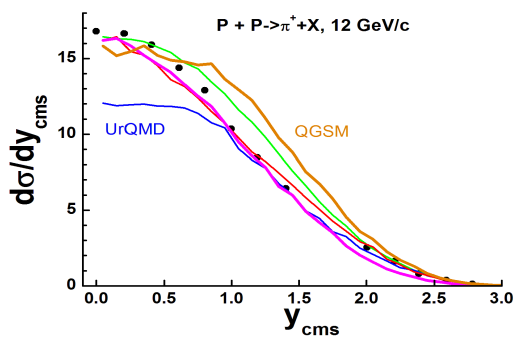
Probabilities of diffractions in Fritiof are not right! The separation allows to fit the probabilities.



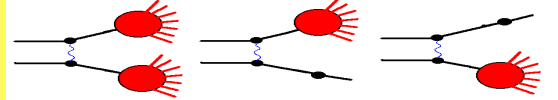


Exp. Data: V. Blobel et al., Nucl. Phys., B69(1974) 454.

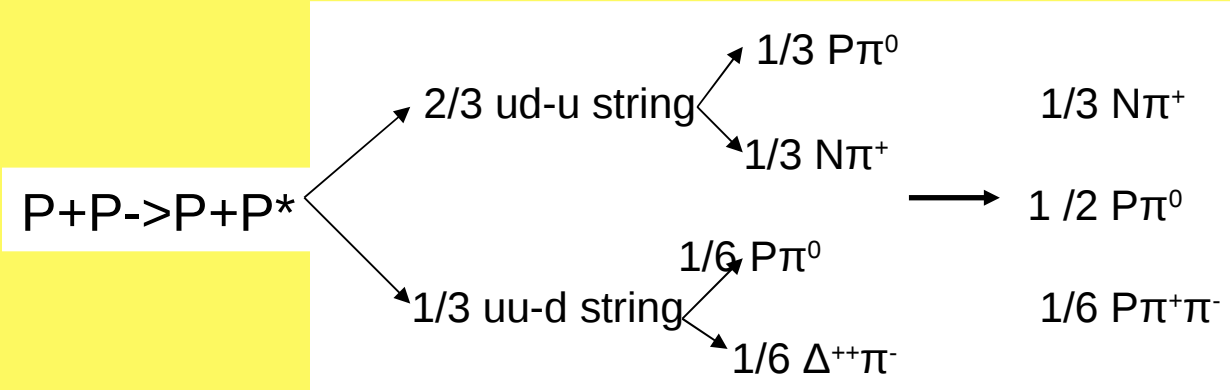
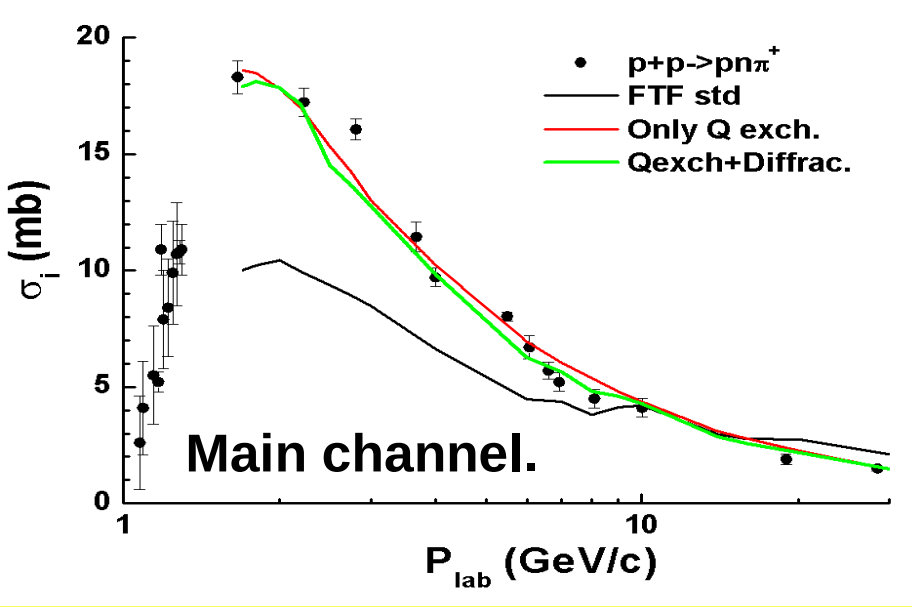
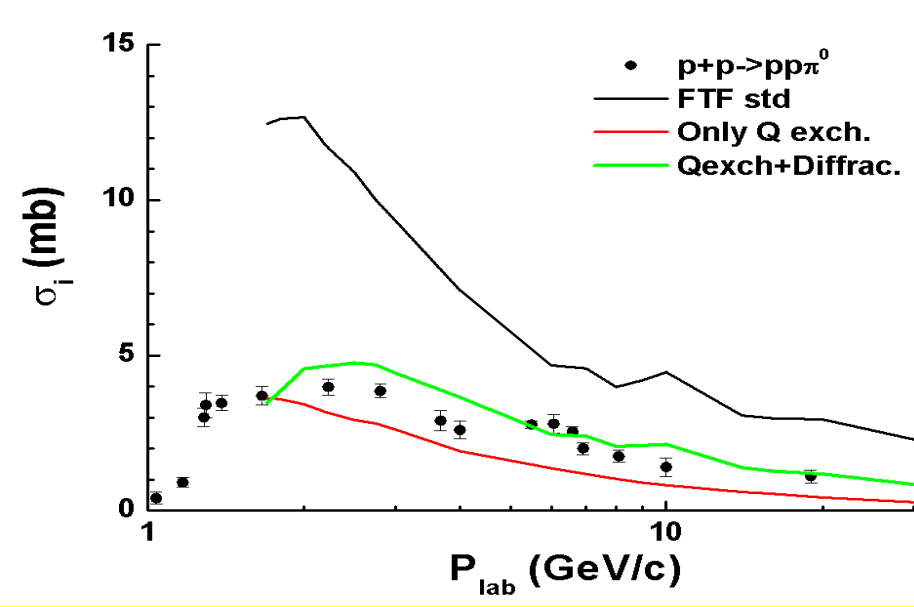
There are some problems with a description of meson spectra



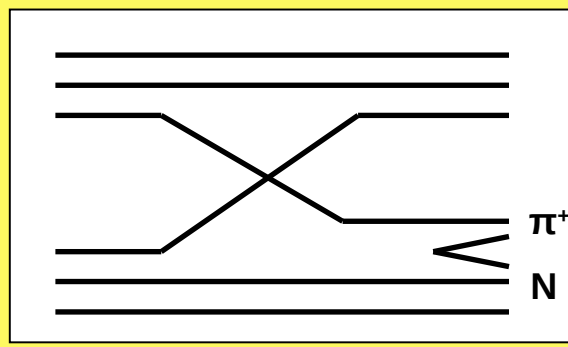
3. Simulation of binary reactions



Standard FTF approach does not give positive results

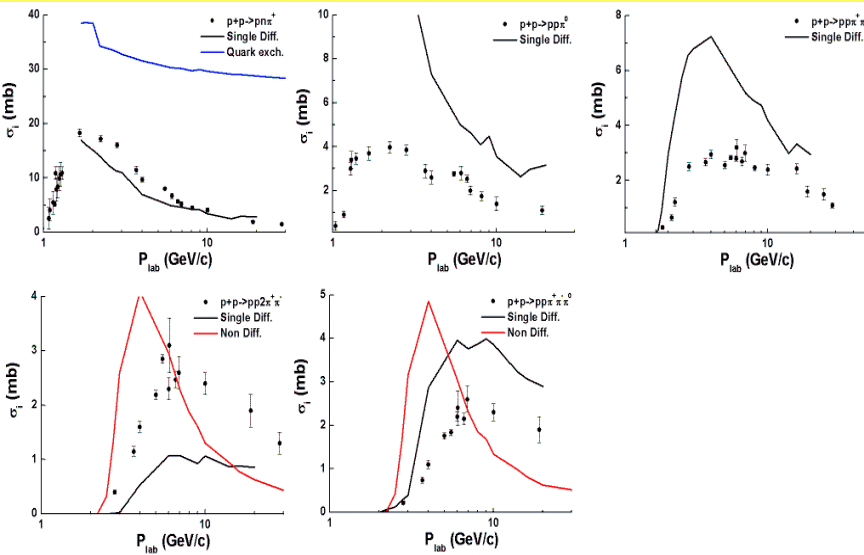


Solution – quark exchange

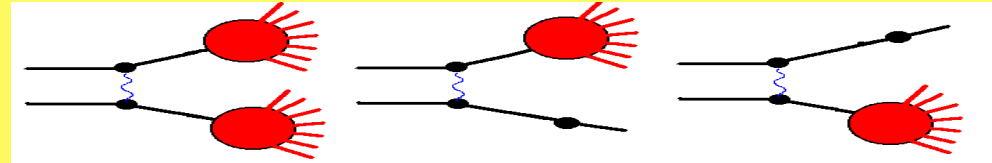


$W_{q.exc.} \sim 3.4 e^{-1.2 \cdot (y_{pr} - y_{tr})}$

~~$P+P \rightarrow P\Delta^+, N\Delta^{++}, \Delta\Delta$~~



Separate simulation of the single diffraction and non-diffraction interactions.



pp → ppπ⁺π⁻

Final state: single diffraction

P(Δ⁺⁺π⁻) XXX

P(Δ⁰π⁺) X

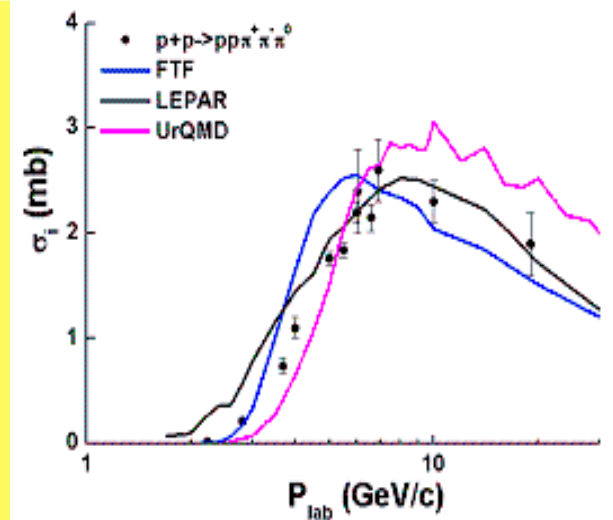
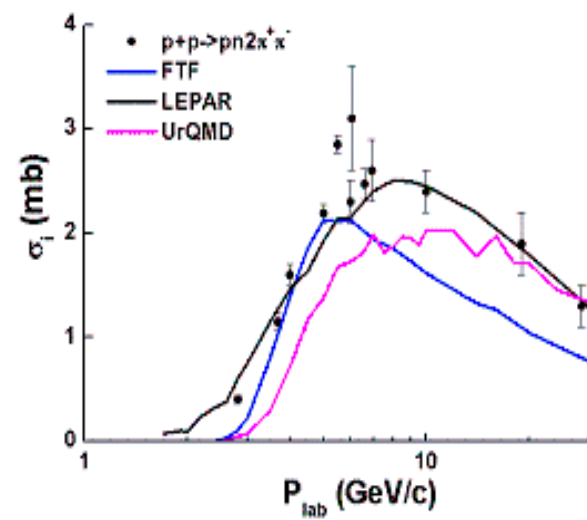
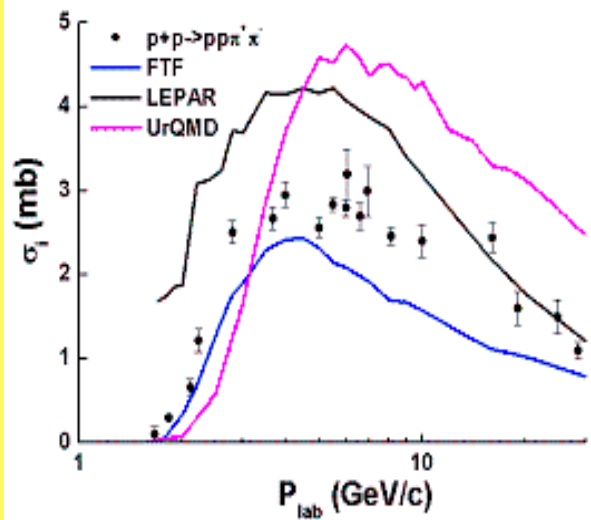
P(Pπ⁺π⁻) 3

SplitLast

Too many delta's!

P(B3/2)=P(B1/2)?

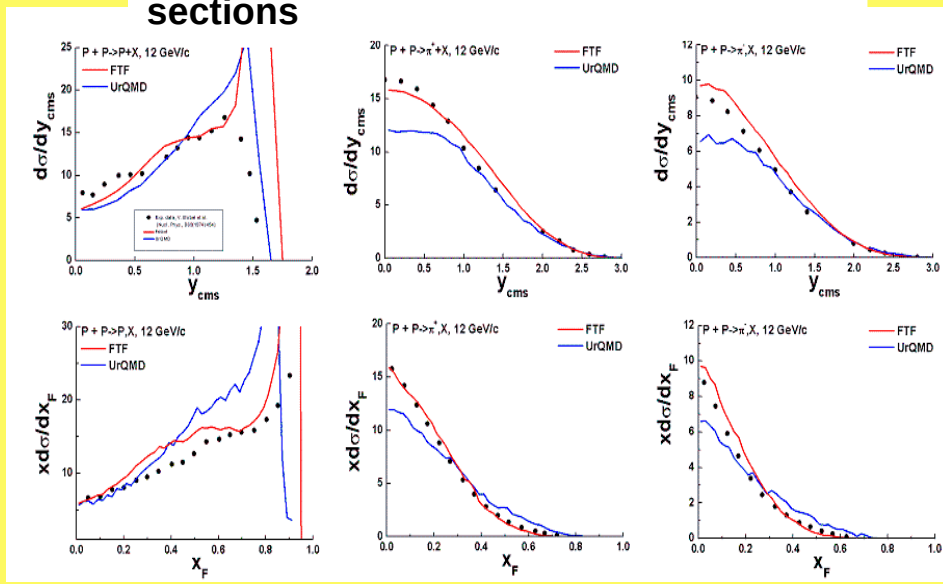
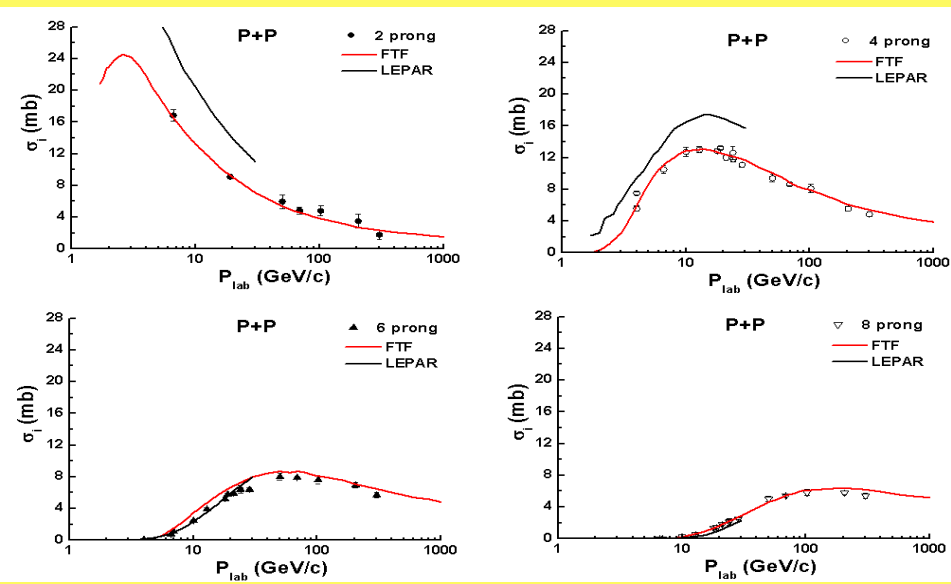
Solution: probability of a final state is proportional to PS~q_{2 part. decay}



PP interaction, channel cross sections

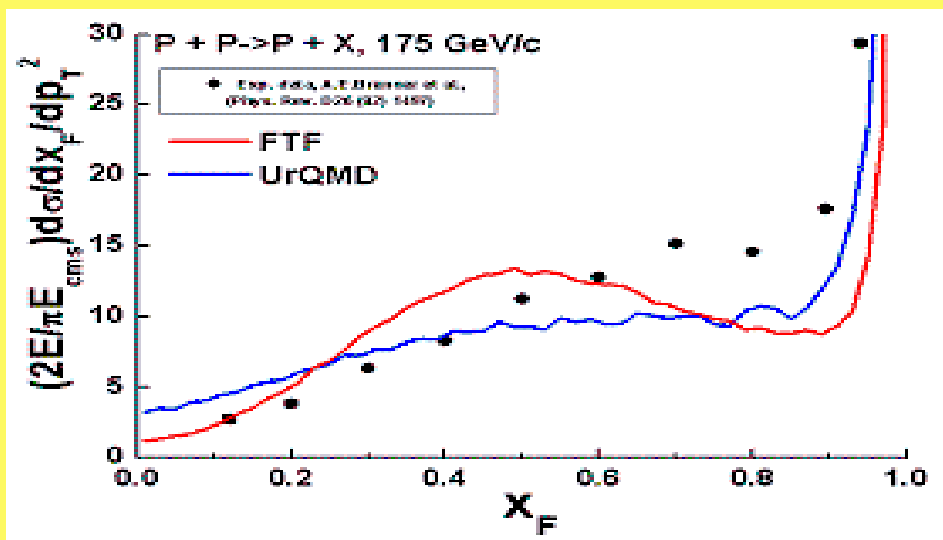
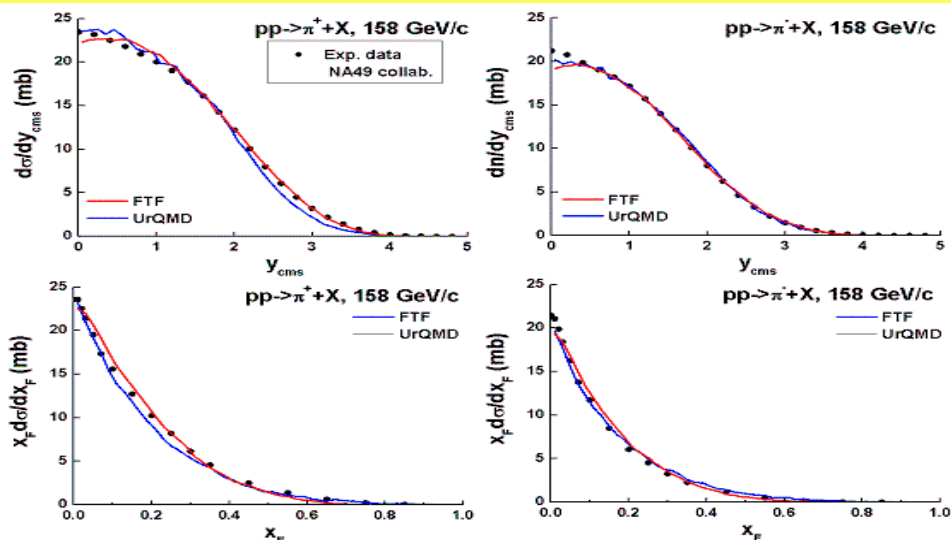
Phase space restrictions at low mass string fragmentation

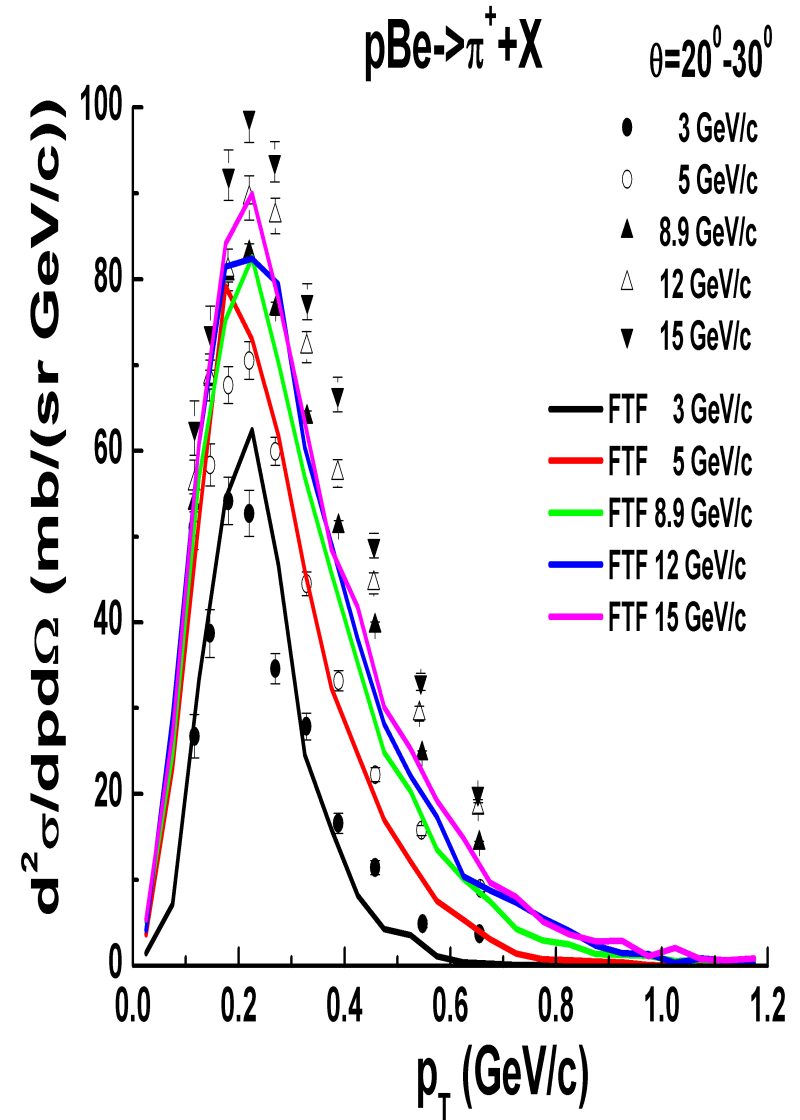
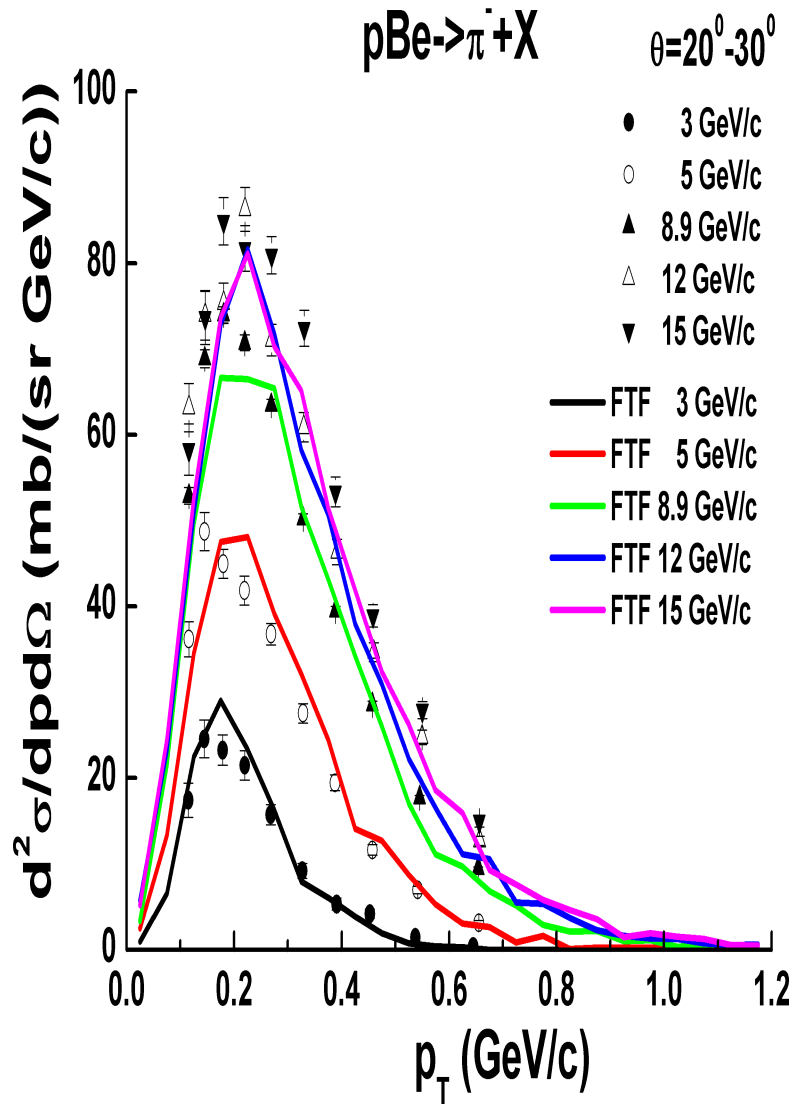
PP interaction, topological cross sections **Results for PP** PP interaction, inclusive cross sections



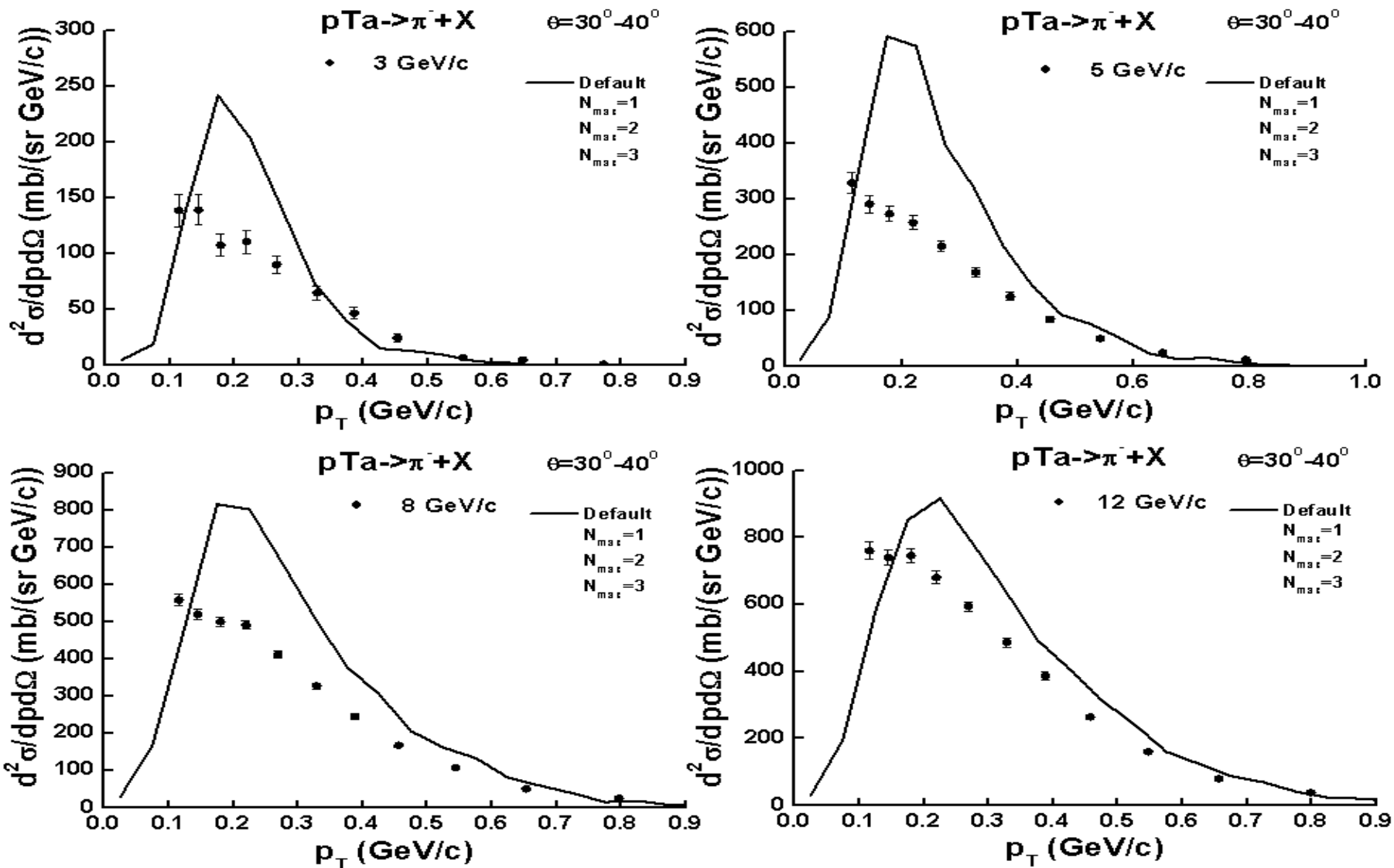
PP interaction, inclusive cross sections

Some problems with proton spectra





Check of inclusive cross sections for PN interactions, HARP-CDP data



PROBLEM!

What can we do?

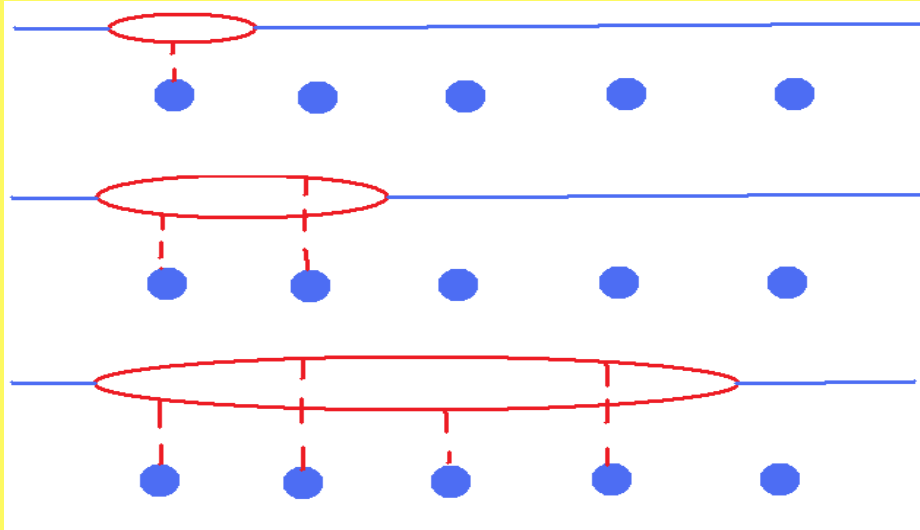
- Change string fragmentation.
- Change string mass distribution.
- Change cross sections.
- Correct interaction number.

Source of the problem: the AGK cutting rules are asymptotical ones!

Glauber cross section

$$\sigma_{pA}^{in} = \int d^2b [1 - e^{-\sigma_{pn}^{in} T(\vec{b})}] = \sum_{\nu=1}^{\infty} \int d^2b \frac{[-\sigma_{pn}^{in} T(\vec{b})]^\nu}{\nu!} e^{-\sigma_{pN} T(\vec{b})}$$

AGK rules



Low energy, Std. cascade.

Cascade+ QGS

High energy, Std. QGS.

Competition of planar and non-planar diagrams. There was only 1 paper on the subject by K. Boreskov and A. Kaidalov.

$$N_{max} = \sigma \rho < \tau > v \gamma = \sigma \rho < \tau > P_{lab}^{proj} / m_{proj}$$

Glauber cross section

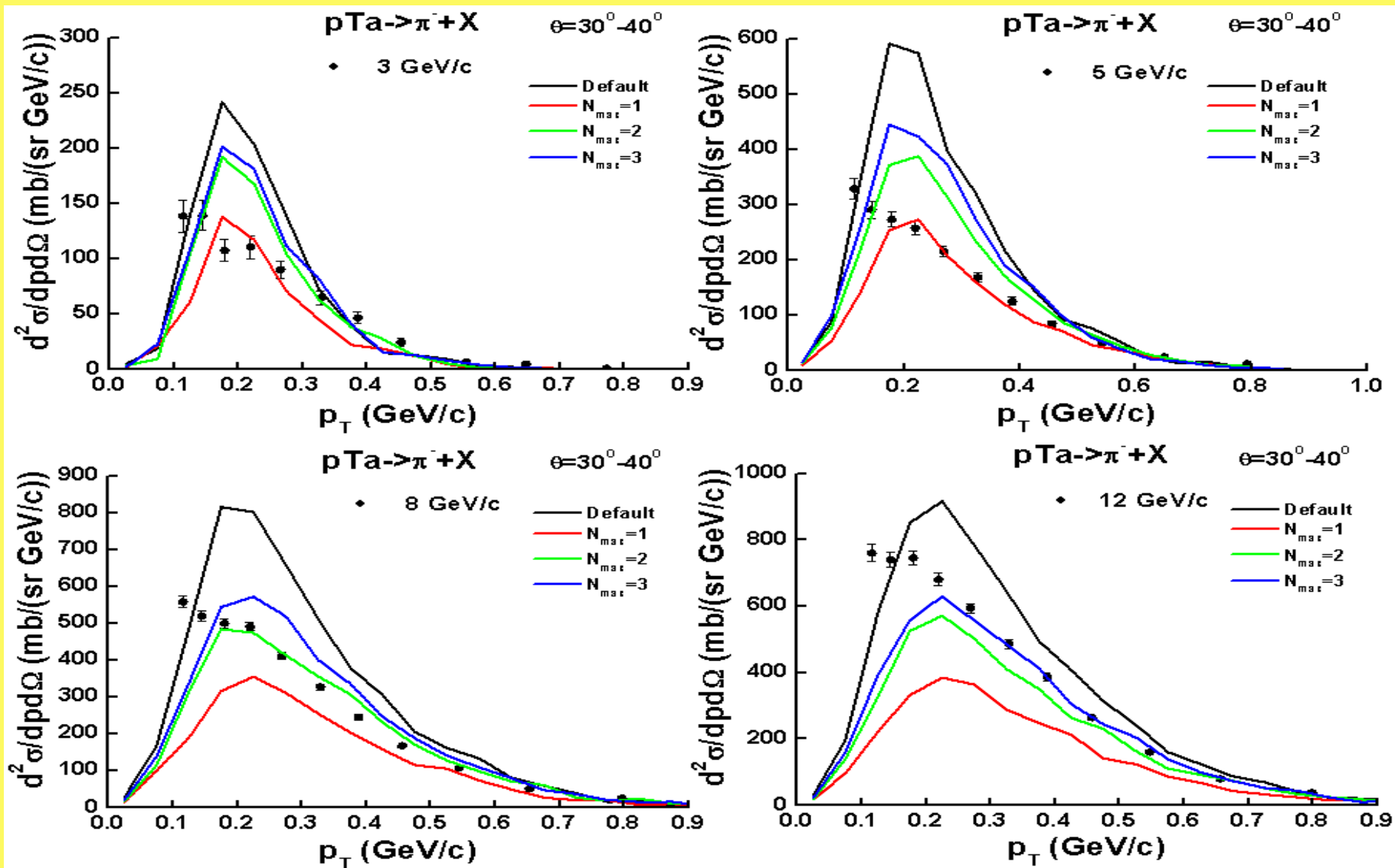
$$\sigma_{pA}^{in} = \int d^2b [1 - e^{-\sigma_{pn}^{in} T(\vec{b})}] = \int d^2b [1 - e^{-N_{max} \frac{\sigma_{pn}^{in}}{N_{max}} T(\vec{b})}] = \sum_{\nu=1}^{N_{max}} C_{N_{max}}^\nu \int d^2b [1 - e^{-\frac{\sigma_{pn}^{in}}{N_{max}} T(\vec{b})}]^\nu e^{-(N_{max}-\nu) \frac{\sigma_{pn}^{in}}{N_{max}} T(\vec{b})}$$

S.Yu. Shmakov, V.V. Uzhinsky, Zeit. fur Phys. C36:77,1987.

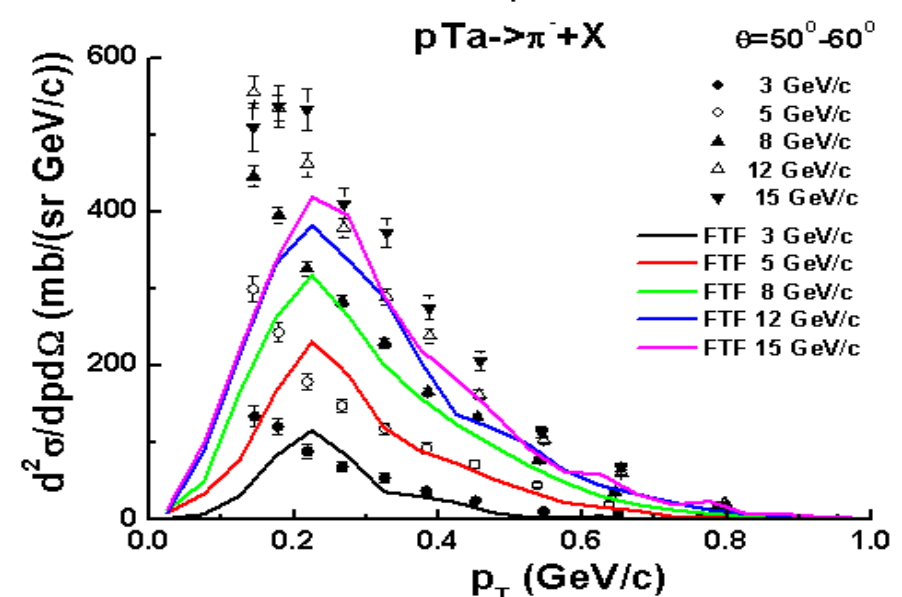
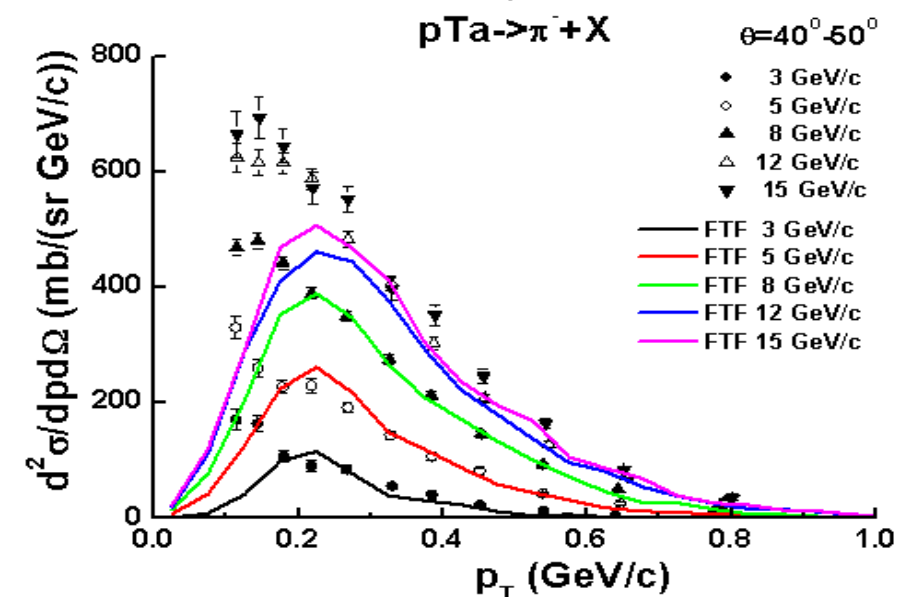
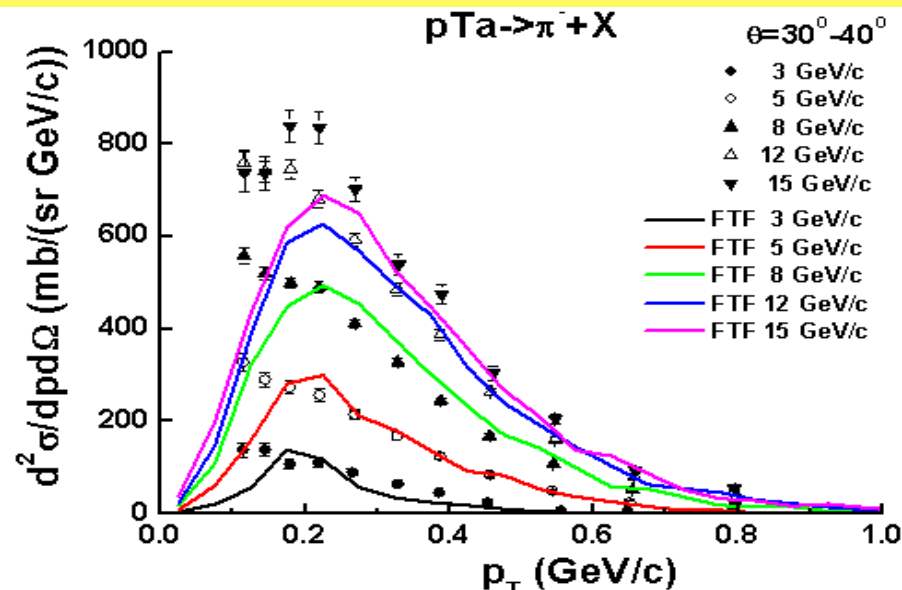
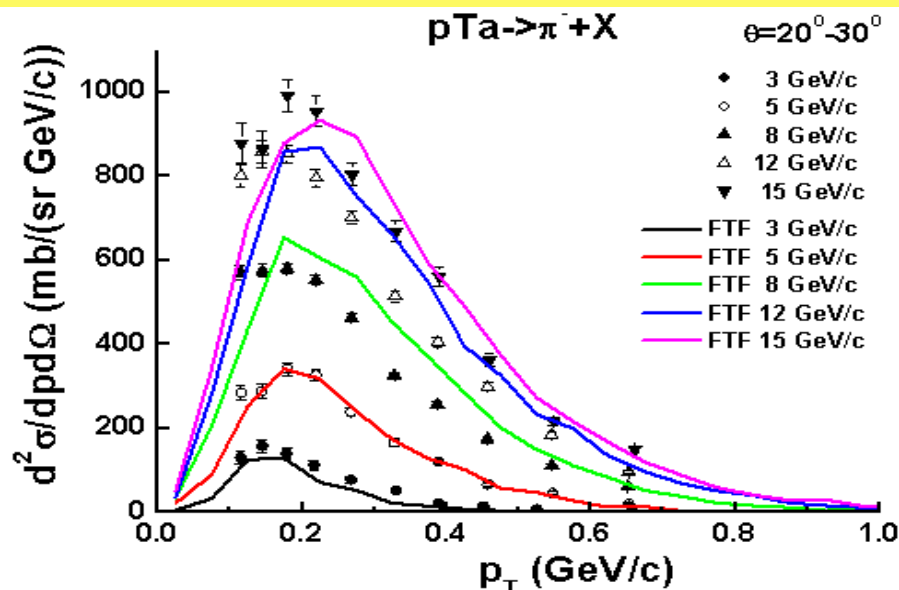
Max. cross section method:

W.A. Coleman: Nucl. Sci. Eng. 32 (1968) 76

Uzhi rules



$N_{\text{max}}=1$, $P_{\text{lab}}=3, 5$ GeV/c: $N_{\text{max}}=2$, $P_{\text{lab}}=8$ GeV/c: $N_{\text{max}}=3$, $P_{\text{lab}}=12$



All O.K. with Pi-mesons!

$N_{max} = P_{lab}/4$ (GeV/c)

Glauber approach implemented in FTF and QGS is not sufficient for a destruction of a nucleus. Thus a reggeon cascading model of nuclear destruction was applied.

Model of nuclear disintegration in high-energy nucleus nucleus interactions.

K. Abdel-Waged, V.V. Uzhinsky

Phys Atom Nucl 60:929-940 1997, Yad Fiz 60:925-937 1997

$$Y = G \int d\xi' d^2b' F_{N\pi}(\vec{b} - \vec{b}', \xi - \xi') \times F_{\pi N}(\vec{b}' - \vec{s}_1, \xi') F_{\pi N}(\vec{b}' - \vec{s}_2, \xi')$$

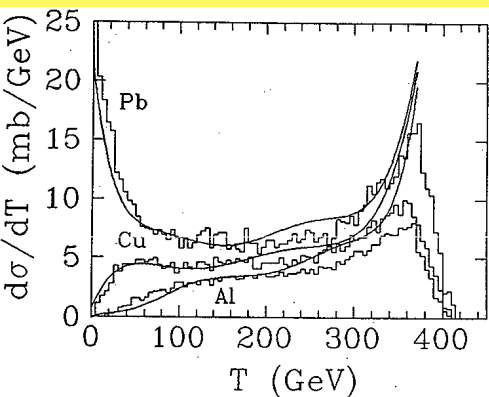
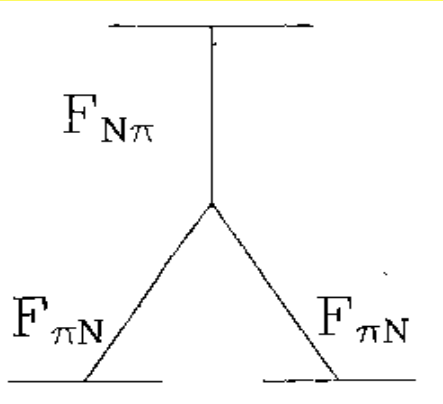
G is 3-pomeron vertex constant, \vec{b} - impact parameter of incident hadron, \vec{s}_1, \vec{s}_2 - impact coordinates of nuclear nucleons. \vec{b}' is the position of pomeron interactions vertex in the impact parameter plane, ξ' -its rapidity.

Using Gaussian parameterization for $F_{\pi N}$ ($F_{\pi N} = \exp(-(|\vec{b}|^2)/(R_{\pi N}^2))$) and neglecting its dependence on energy, we have

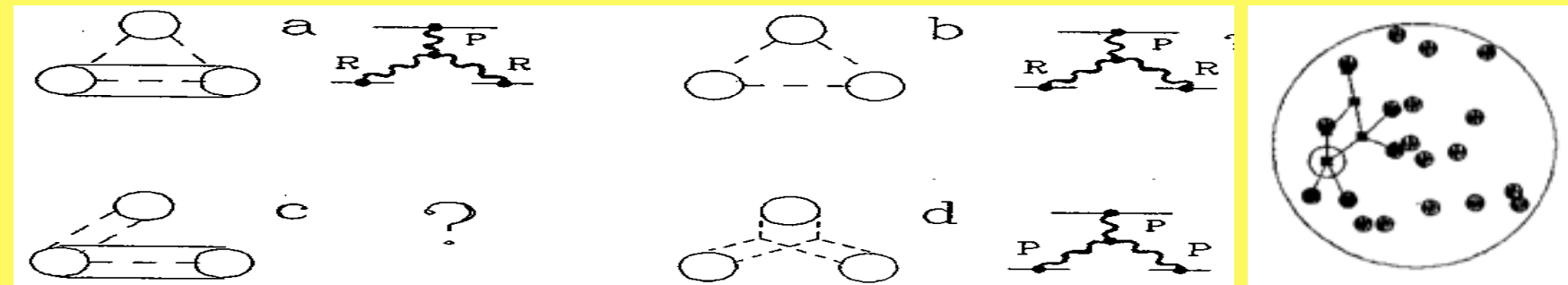
$$Y \simeq G(\xi_0 - 2\epsilon) \frac{R_{\pi N}^2}{3} \exp(-(\vec{b} - (\vec{s}_1 + \vec{s}_2)/2)^2 / 3R_{\pi N}^2) \times \exp(-(\vec{s}_1 - \vec{s}_2)^2 / 2R_{\pi N}^2),$$

where $R_{\pi N}$ is the pion-nucleon interaction radius. According to (2) the contribution reaches a maximum if the nucleon coordinates \vec{s}_1 and \vec{s}_2 coincide and decreases very fast with increasing the distance between the nucleons. For reproduction of this behavior we choose ϕ as

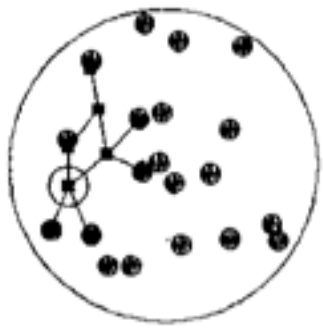
$$\phi(|\vec{s}_i - \vec{s}_j|) = C \exp(-\frac{|\vec{s}_i - \vec{s}_j|^2}{r_c^2}).$$



Si+A, 14.7 GeV/N
T – energy in ZDC



How have we to determine momentum spectra of nucleons?



Complex analysis of gold interactions with photoemulsion nuclei at 10.7-GeV/nucleon within the framework of cascade and FRITIOF models.

By EMU-01 Collaboration (M.I. Adamovich *et al.*), 1997. Zeit. fur Phys.A358:337-351,1997.

In case of dissociation of two compound systems A and B containing A and B constituents respectively, the i -th constituent of system A will be described by

$$x_i^- = (E_{A_i} + p_{i3})/W_A^- \quad \text{and} \quad q_{i1},$$

and the j -th constituent of system B

$$x_j^- = (E_{B_j} + q_{j3})/W_B^- \quad \text{and} \quad q_{j1}.$$

Here, $E_{A_i}(E_{B_j})$ and $p_{i3}(q_{j3})$ are energy and momentum of i -th constituent from $A(B)$.

$$W_A^- = \sum_{i=1}^A (E_{A_i} + p_{i3}), \quad W_B^- = \sum_{j=1}^B (E_{B_j} + q_{j3}).$$

Using these variables, let us write the conservation law as

$$\begin{aligned} W_A^- + \frac{1}{2} W_A^+ &= \sum_{i=1}^A \frac{m_{i\perp}^2}{x_i^-} + W_B^- + \frac{1}{2} W_B^+ \sum_{j=1}^B \frac{\mu_j^2}{y_j^-} \\ &= E_A^0 + E_B^0, \\ \frac{W_A^-}{2} - \frac{1}{2W_A^+} \sum_{i=1}^A \frac{m_{i\perp}^2}{x_i^-} &= \frac{W_B^-}{2} + \frac{1}{2W_B^+} \sum_{j=1}^B \frac{\mu_j^2}{y_j^-} \\ &= E_A^0 + E_B^0, \\ \sum_{i=1}^A p_{i1} + \sum_{j=1}^B q_{j1} &= 0, \end{aligned} \quad (15)$$

where $m_{i\perp}^2 = m_i^2 + p_{i\perp}^2$, $\mu_j^2 = m_j^2 + q_{j\perp}^2$, and m_i, m_j - mass of the constituent from system $A(B)$.

System (15) allows us to determine W_A^+, W_B^+ and kinematic characteristics of all the particles in the finite sets $\{x_i^-, p_{i1}\}$, $\{y_j^-, q_{j1}\}$.

$$W_A^+ = (W_0^- W_0^+) (\alpha - \beta + \sqrt{\Delta}) / 2W_0^+, \quad (16)$$

$$W_B^+ = (W_0^- W_0^+) (\alpha + \beta + \sqrt{\Delta}) / 2W_0^+, \quad (17)$$

$$W_0^+ = (E_A^0 + E_B^0) + (E_{A_0}^0 + E_{B_0}^0);$$

$$W_0^- = (E_A^0 + E_B^0) - (E_{A_0}^0 - E_{B_0}^0);$$

$$\alpha = \sum_{i=1}^A \frac{m_{i\perp}^2}{x_i^-}, \quad \beta = \sum_{j=1}^B \frac{\mu_j^2}{y_j^-};$$

$$\Delta = (W_0^- W_0^+)^2 + \alpha^2 - \beta^2 - 2W_0^- W_0^+ \alpha - 2W_0^- W_0^+ \beta - 2\alpha\beta;$$

$$p_{i1} = (W_A^+ x_i^- - \frac{m_{i\perp}^2}{x_i^-}) / 2; \quad q_{j1} = (W_B^+ y_j^- - \frac{\mu_j^2}{y_j^-}) / 2.$$

To reproduce this result the values of $\mathbf{p}_{i\perp}$ for knocked-out nucleons are simulated according to distribution

$$dW \propto \exp(-\mathbf{p}_{i\perp}^2 / \langle p_{\perp}^2 \rangle) d^2 p_{i\perp}, \quad \sqrt{\langle p_{\perp}^2 \rangle} = 0.05. \quad (18)$$

The sum of transverse momenta (with sign "minus") was ascribed to the residual nucleus.

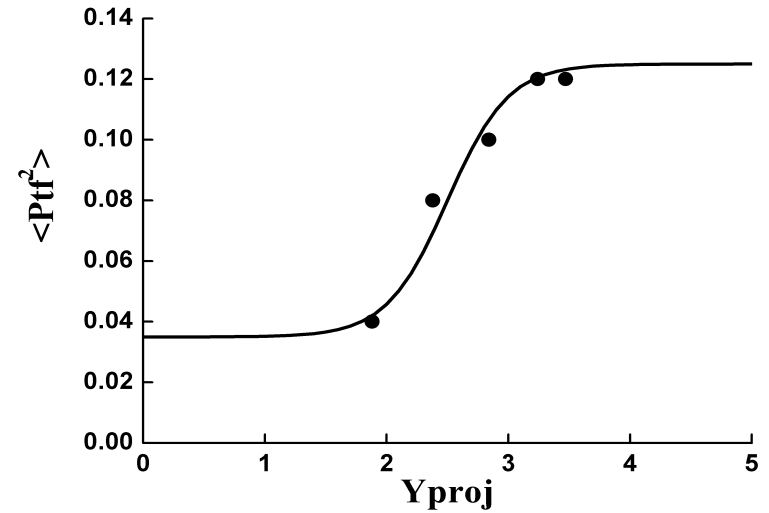
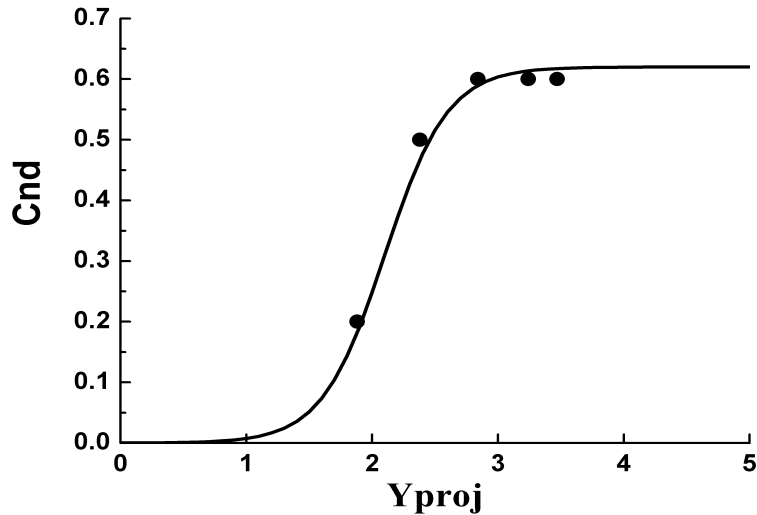
The choice of x_i^+ is carried out by

$$dW \propto \exp[-(x_i^+ - 1/A)^2 / (d_x/A)^2] dx_i^+, \quad d_x = 0.05. \quad (19)$$

The dispersion of the distribution was defined by fitting the average emission angle of b -particles. x^+ of the residual nucleus was included as $1 - \sum x_i^+$.

Main parameters: C_{nd} , d_x , p_T^2

Unexpected results of the tuning!



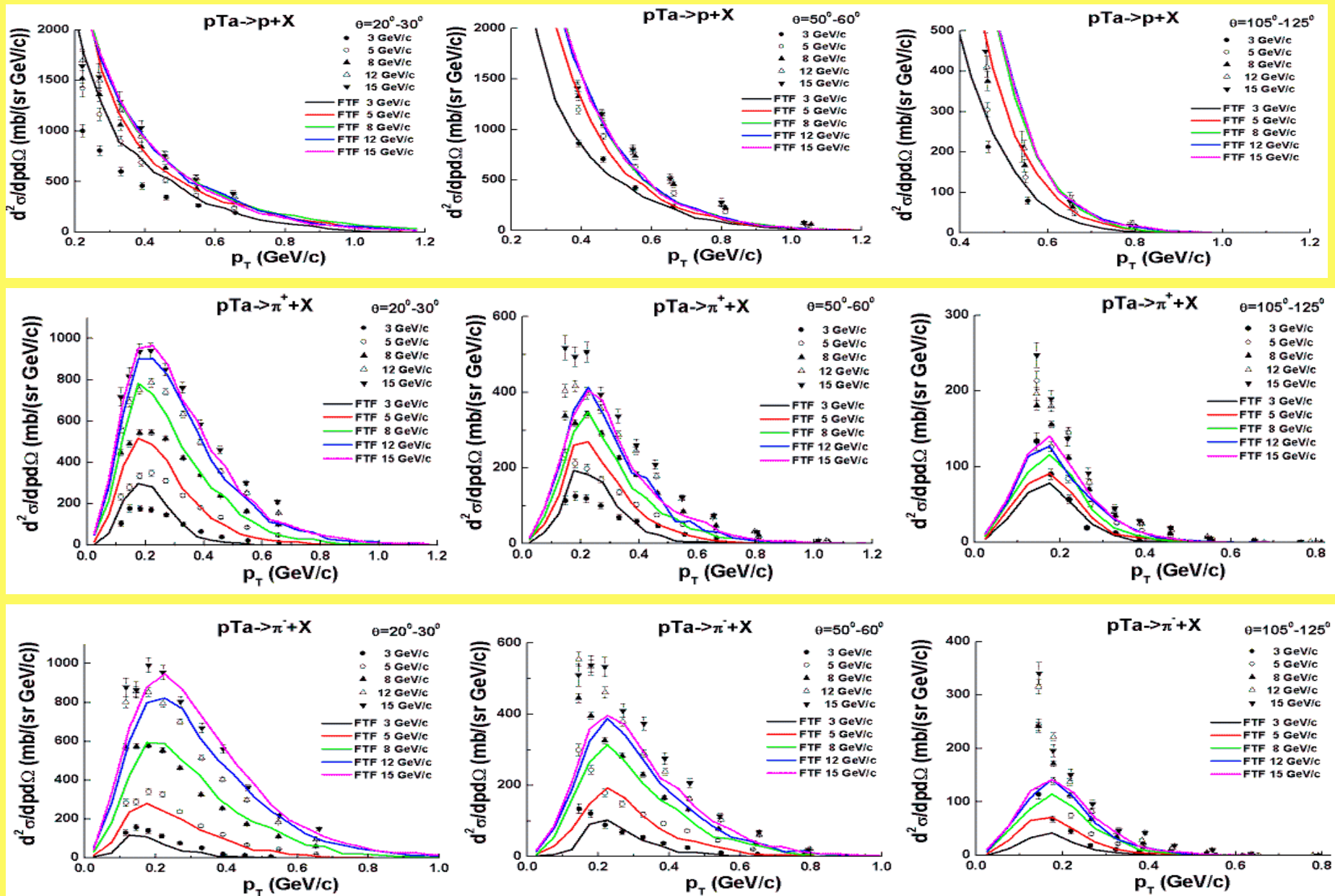
$$C_{nd} = 0.62 \frac{e^{4(y-2.1)}}{1 + e^{4(y-2.1)}}$$

$$y = 2.1 \text{ at } p_{lab} \simeq 4 \text{ GeV}/c$$

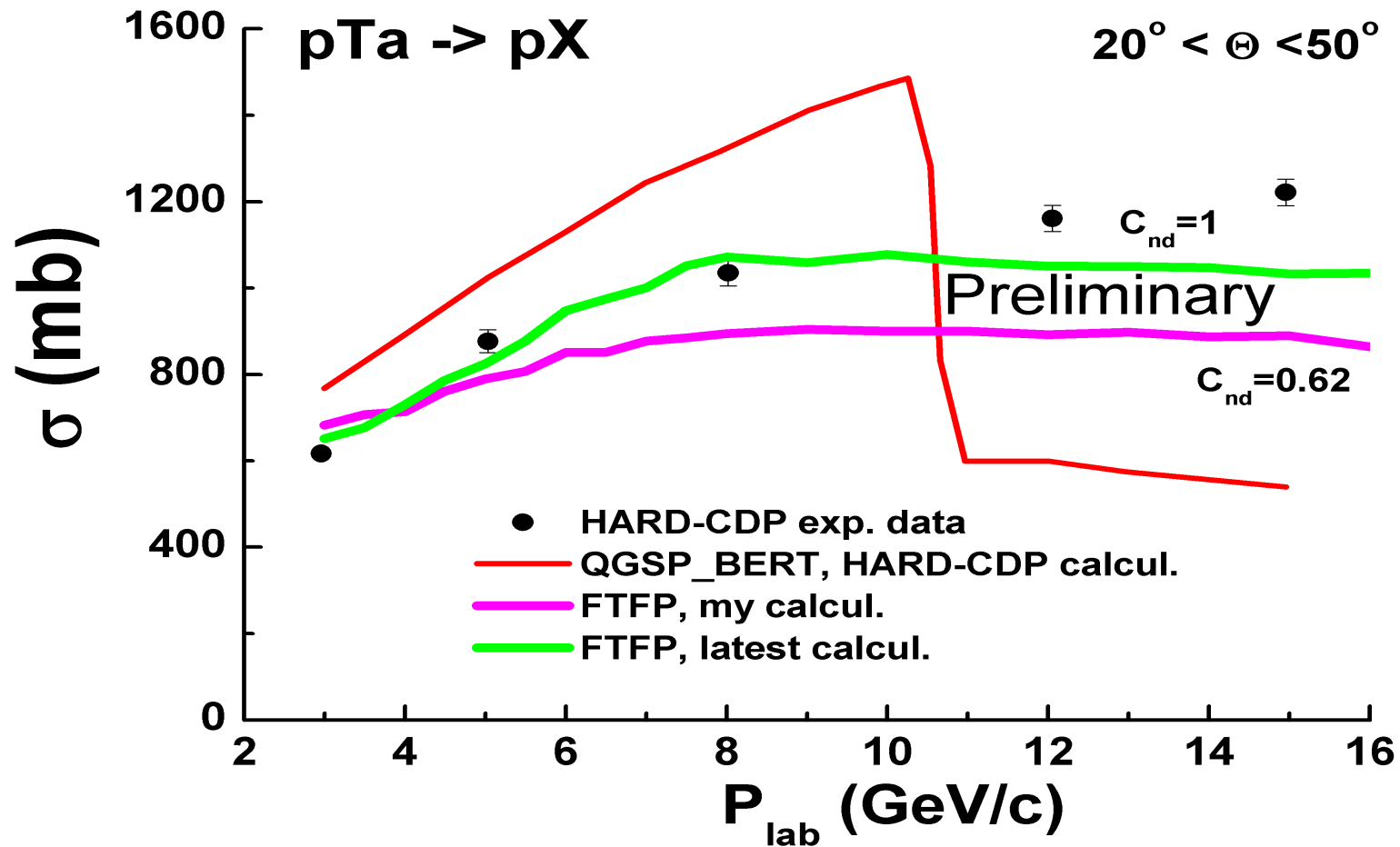
$$\langle P_T^2 \rangle = 0.035 + 0.09 \frac{e^{4(y-2.5)}}{1 + e^{4(y-2.5)}} \text{ (GeV}/c)^2$$

$$y = 2.5 \text{ at } p_{lab} \simeq 5.5 \text{ GeV}/c$$

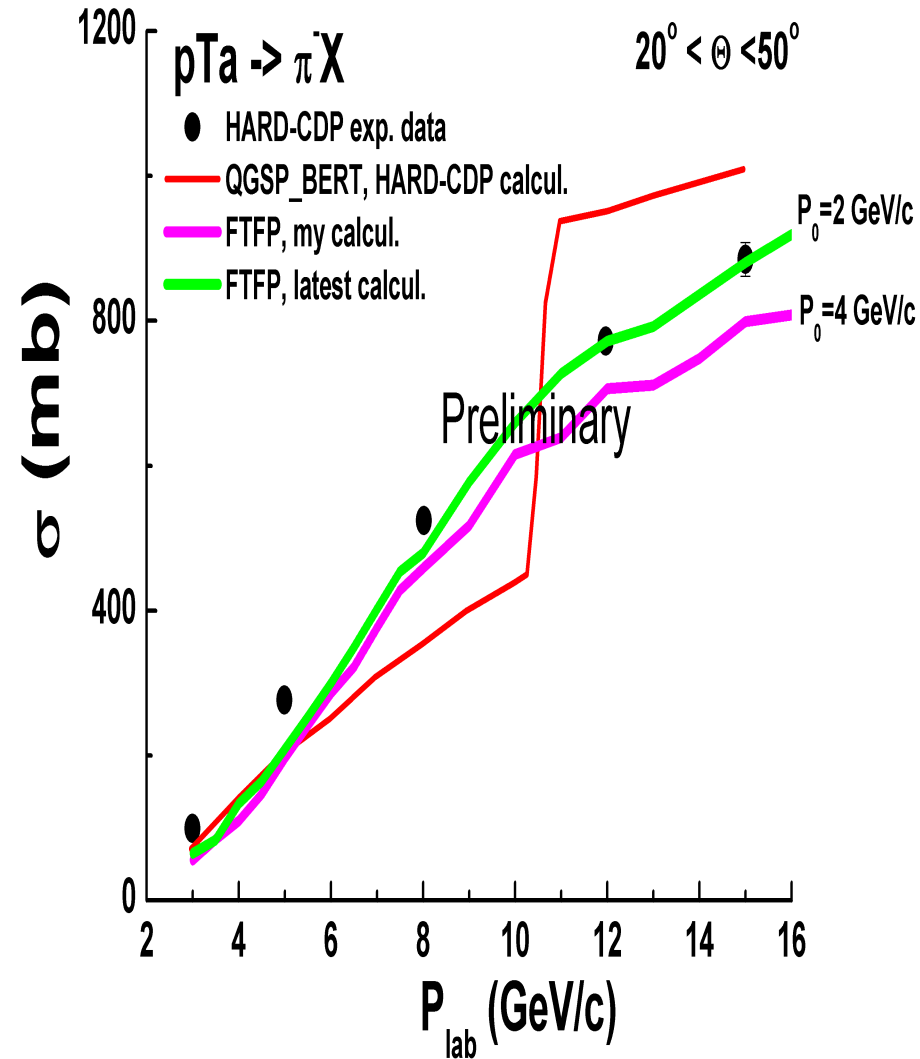
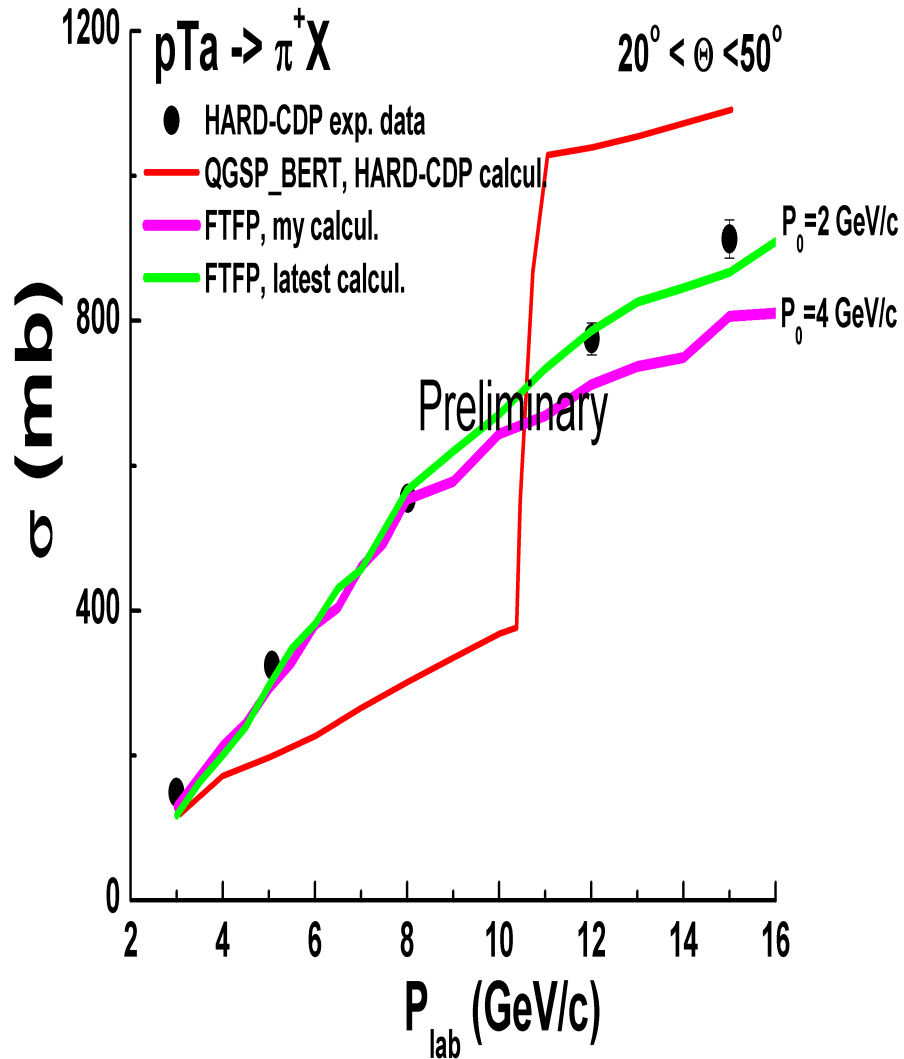
**Clear signal of a transition regime!
The transition takes place at $P_{lab} = 4-5 \text{ GeV}/c$**



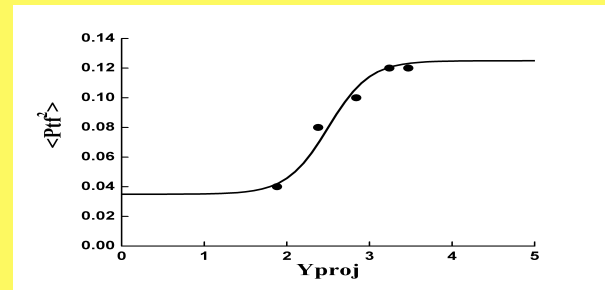
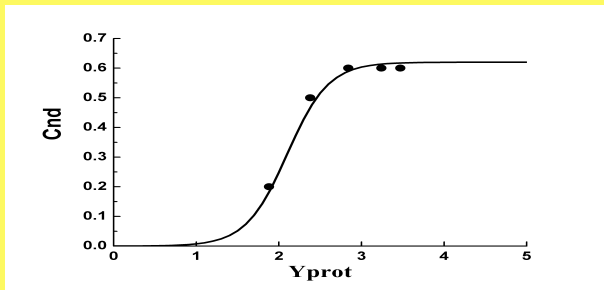
All is beautiful!



HARP-CDP hadroproduction data: Comparison with FLUKA and GEANT4 simulations.
HARP-CDP Collaboration (A. Bolshakova *et al.*) CERN-PH-EP-2010-017, Jun 2010. 21pp.
Submitted to Eur.Phys.J.C, e-Print: arXiv:1006.3429 [hep-ex]



- New things are introduced in FTF for pp- and pA-interactions:**
 - Separate simulation of diffractive and non-diffractive interactions
 - Phase space restrictions at low mass string fragmentation
 - Quark exchange for simulation of binary reactions
 - Correction of multiplicity of intra-nuclear collisions
 - RTIM was implemented and its parameters were tuned
- Good results are obtained for pp- and pA-interactions, especially for description of the HARP-CDP data. The description of the HARP-CDP data on pA-interactions (Be, C, Cu, Ta, Pb) is the best among other models!**
- A strong indication on transition regime realization is obtained!**



**Improved FTF model will be in December release of Geant4.
It will be considered as production model.**

Possible experimental check

