

Geant 4

*Detector Description:
Sensitive Detector & Field*

<http://cern.ch/geant4>

PART III

Detector Sensitivity

- *Sensitive detectors*
- *Primitive scorers*
- *Hits & digits*
- *Read-out geometry*

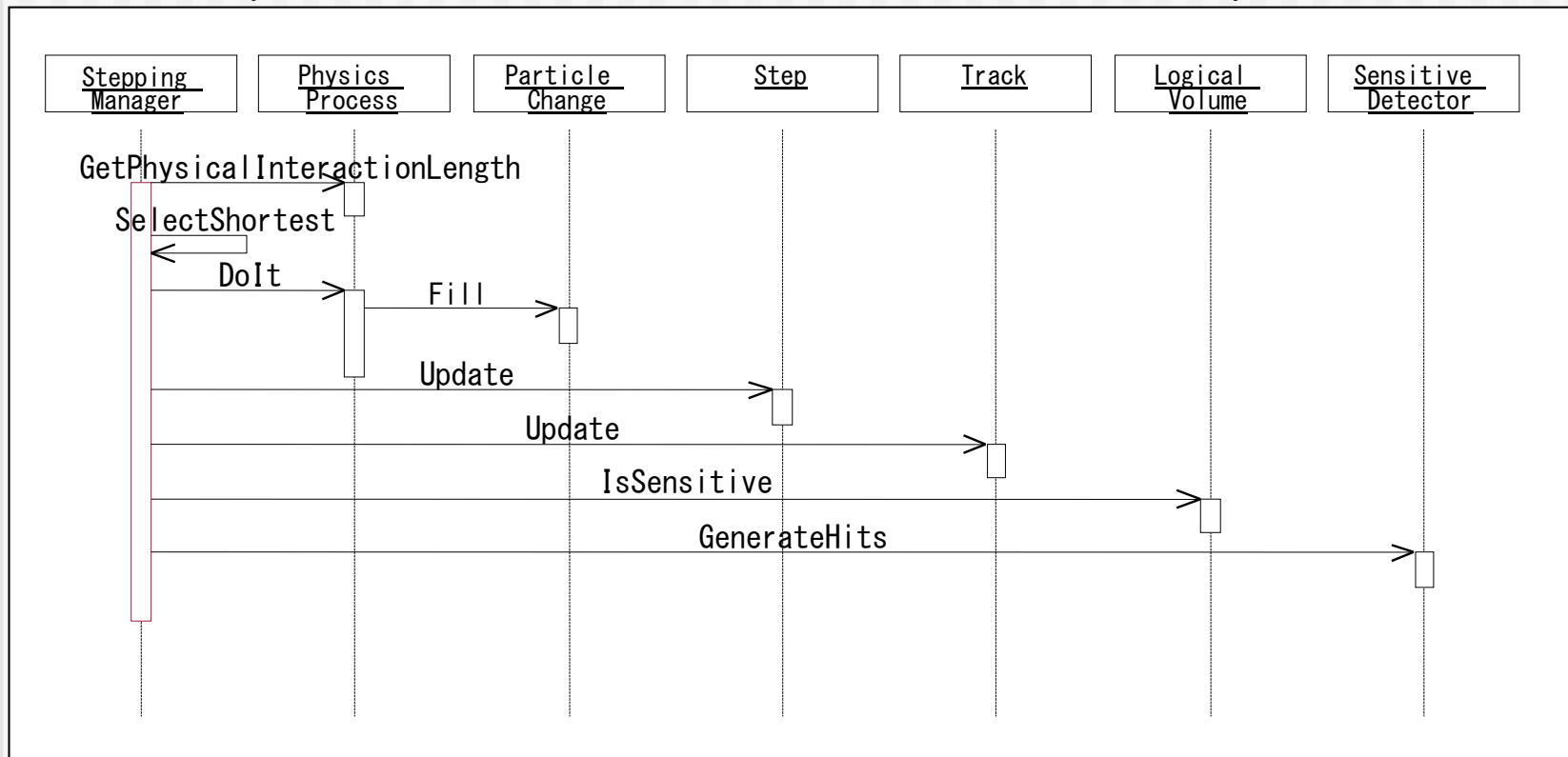
Detector sensitivity

- A logical volume becomes sensitive if it has a pointer to a concrete class derived from **G4VSensitiveDetector**
- A sensitive detector either
 - constructs one or more hit objects or
 - accumulates values to existing hitsusing information given in a **G4Step** object

NOTE: you must get the volume information from the "**PreStepPoint**"

Sensitive Detector

- A `G4VSensitiveDetector` object should be assigned to `G4LogicalVolume`
- In case a step takes place in a logical volume that has a Sensitive Detector object, the Sensitive Detector is invoked with the **current `G4Step`** object.
 - Either implement dedicated sensitive detector classes, or use predefined **scorers**



Provided Primitive Scorers

■ Track length

- `G4PSTrackLength`, `G4PSPassageTrackLength`

■ Deposited energy

- `G4PSEnergyDeposit`, `G4PSDoseDeposit`, `G4PSChargeDeposit`

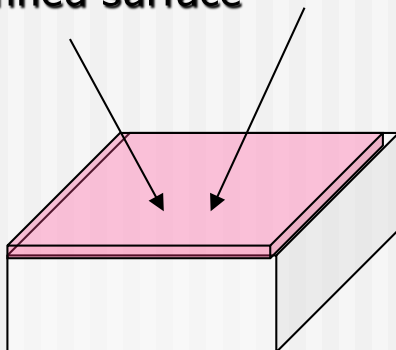
■ Current/Flux

- `G4PSFlatSurfaceCurrent`, `G4PSSphereSurfaceCurrent`, `G4PSPassageCurrent`,
`G4PSFlatSurfaceFlux`, `G4PSCellFlux`, `G4PSPassageCellFlux`

- **Others:** `G4PSMinKinEAtGeneration`, `G4PSNofSecondary`, `G4PSNofStep`, ...

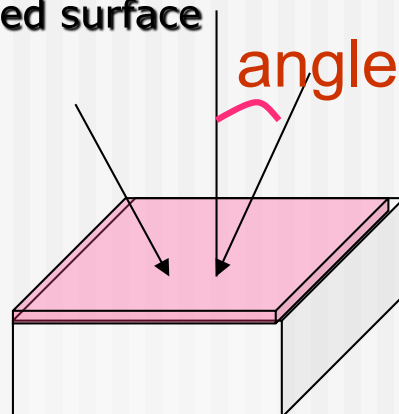
SurfaceCurrent :

Count number
of injecting
particles at
defined surface



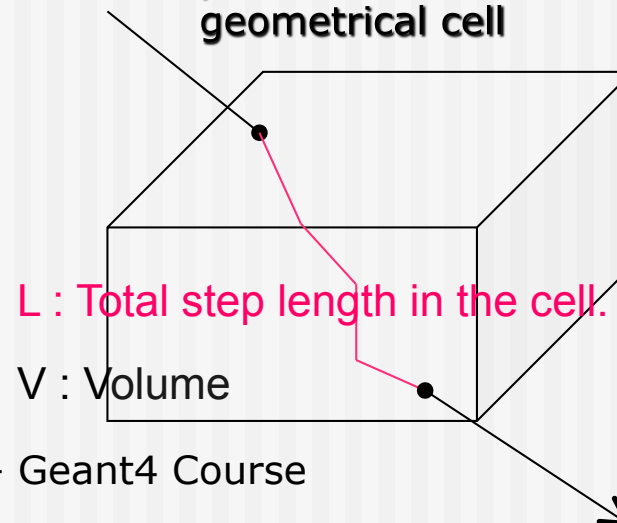
SurfaceFlux :

Sum up $1/\cos(\text{angle})$
of injecting particles
at defined surface



CellFlux :

Sum of L / V of injecting
particles in the
geometrical cell



Sensitive Detector vs. Primitive Scorer

Sensitive detector

- User must implement his/her own detector and hit classes
- One hit class can contain many quantities. A hit can be made for each individual step, or accumulate quantities
- Basically one hits collection is made per one detector
- Hits collection is relatively compact

➤ Use primitive scorers

- ▶ if **not** interested in recording each individual step **but** accumulating some physics quantities for an event or a run, and
- ▶ if do **not** need too many of them
- ▶ Otherwise... consider implementing your own sensitive detector

Primitive scorer

- Many predefined scorers are provided in Geant4. One can add his own
- Each scorer accumulates a quantity for each event
- **G4MultiFunctionalDetector** creates many collections (maps), i.e. one collection per one scorer
- Keys of maps are redundant for scorers of same volume

Sensitive detector and Hit

- Each “Logical Volume” can have a pointer to a sensitive detector
- Hit is a snapshot of the physical interaction of a track or an accumulation of interactions of tracks in the sensitive region of your detector
- A sensitive detector creates hit(s) using the information given in `G4Step` object. The user has to provide his/her own implementation of the detector response
- Hit objects, which still are the user’s class objects, are collected in a `G4Event` object at the end of an event.
 - The `UserSteppingAction` class should NOT do this

Hit class - 1

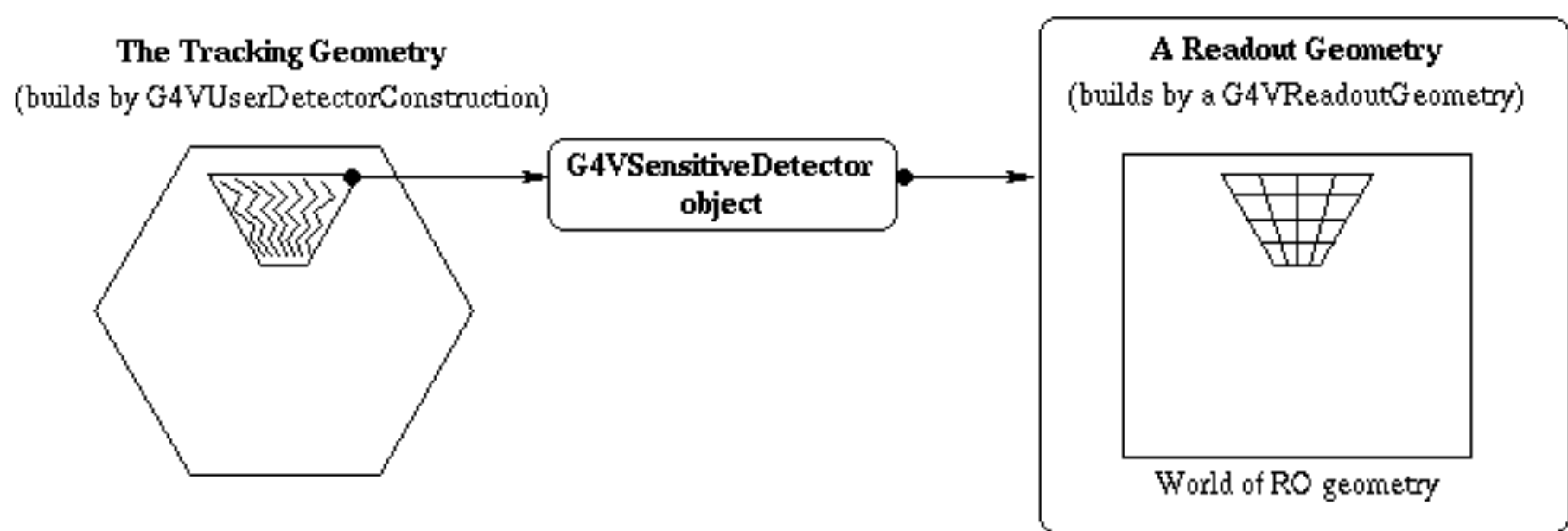
- Hit is a user-defined class derived from `G4VHit`
- You can store various types information by implementing your own concrete Hit class
- For example:
 - Position and time of the step
 - Momentum and energy of the track
 - Energy deposition of the step
 - Geometrical information
 - or any combination of above

Hit class - 2

- Hit objects of a concrete hit class must be stored in a dedicated collection which is instantiated from **G4THitsCollection** template class
- The collection will be associated to a **G4Event** object via **G4HCofThisEvent**
- Hits collections are accessible
 - through **G4Event** at the end of event,
 - through **G4SDManager** during processing an event
 - Used for Event filtering

Readout geometry

- Readout geometry is a virtual and artificial geometry which can be defined in parallel to the real detector geometry
- A readout geometry is optional
- Each one is associated to a sensitive detector



Digitization

- Digit represents a detector output (e.g. ADC/TDC count, trigger signal)
- Digit is created with one or more hits and/or other digits by a concrete implementation derived from **G4VDigitizerModule**
- In contradiction to the Hit which is generated at tracking time automatically, the **digitize()** method of each **G4VDigitizerModule** must be explicitly invoked by the user's code (e.g. **EventAction**)

Defining a sensitive detector

■ Basic strategy

```
G4LogicalVolume* myLogCalor = .....;
G4VSensitiveDetector* pSensitivePart =
    new MyCalorimeterSD ("/mydet/calorimeter");
G4SDManager* SDMan = G4SDManager::GetSDMpointer();
SDMan->AddNewDetector(pSensitivePart);
myLogCalor->SetSensitiveDetector(pSensitivePart);
```

PART III

Magnetic Field

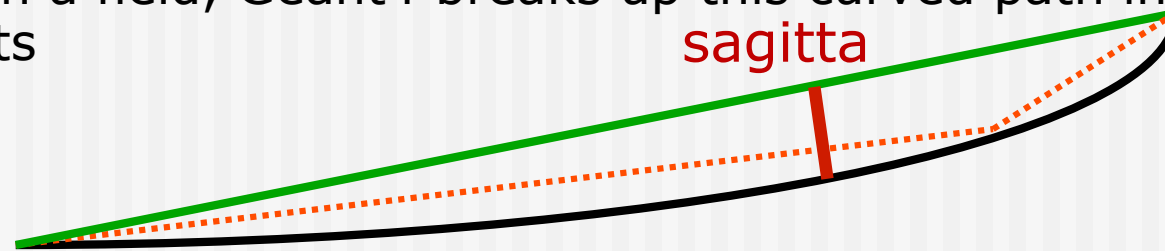
- *Field Propagation & accuracy*
- *Global & Local Field*
- *Tunable parameters*
- *Field Integration*

Field Propagation

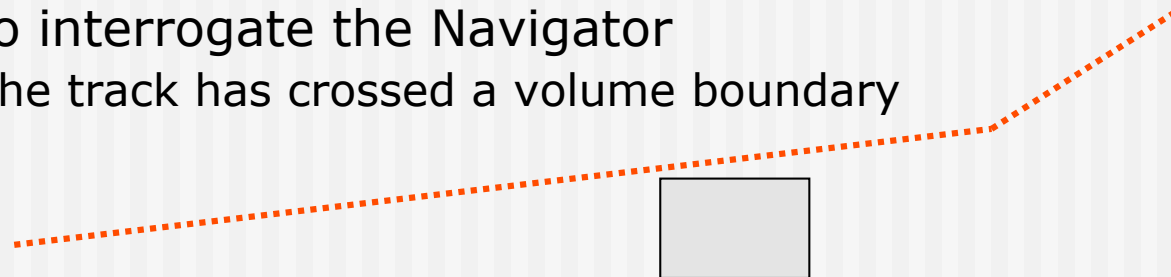
- In order to propagate a particle inside a field (e.g. magnetic, electric or both), we integrate the equation of motion of the particle in the field
- In general this is best done using a **Runge-Kutta** (RK) method for the integration of ordinary differential equations
 - Several RK methods are available
- In specific cases other solvers can also be used:
 - In a uniform field, using the known analytical solution
 - In a nearly uniform but varying field, with RK+Helix

Chords

- Once a method is chosen that allows Geant4 to calculate the track's motion in a field, Geant4 breaks up this curved path into linear chord segments

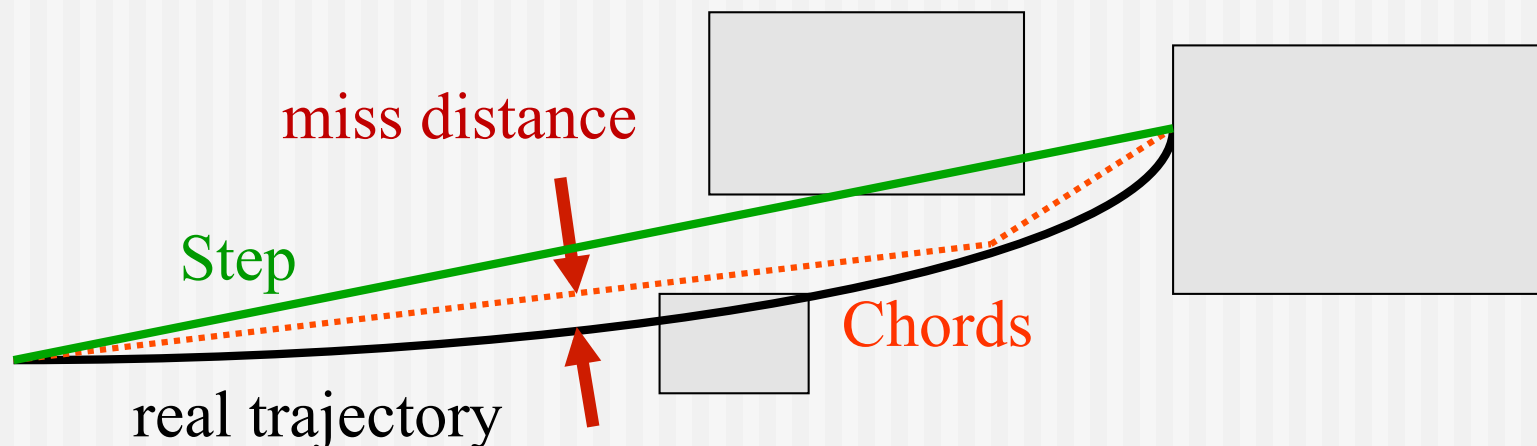


- The chord segments are determined so that they closely approximate the curved path; they're chosen so that their **sagitta** is small enough
 - The *sagitta* is the maximum distance between the curved path and the straight line
 - Small enough: is smaller than a user-defined maximum
- Chords are used to interrogate the Navigator
 - to see whether the track has crossed a volume boundary



Intersection accuracy

- The accuracy of the volume intersection can be tuned
 - by setting a parameter called the "miss distance"
 - The *miss distance* is a measure of the error resolution by which the chord may intersect a volume
 - Default *miss distance* is 0.25 mm
 - Setting small *miss distance* may be highly CPU consuming
- One step can consist of more than one chord
 - In some cases, one step consists of several turns



How to set a Magnetic Field ...

- Magnetic field class
 - Uniform field :
 G4UniformMagField class object
 - Non-uniform field :
 Concrete class derived from **G4MagneticField**
- Set it to **G4FieldManager** and create a Chord Finder

```
G4FieldManager* fieldMgr =  
    G4TransportationManager::GetTransportationManager()  
        ->GetFieldManager();  
fieldMgr->SetDetectorField(magField);  
fieldMgr->CreateChordFinder(magField);
```

Global & Local Fields

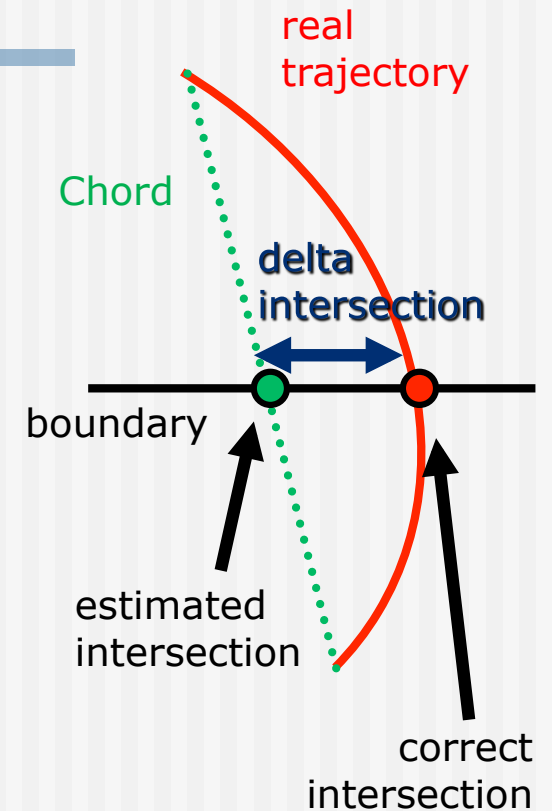
- One field manager is associated with the 'world'
- Other volumes/regions in the geometry can override this
 - An alternative field manager can be associated with any logical volume
 - The field must accept **position in global coordinates** and return **field in global coordinates**
 - The assigned field is propagated to all the daughter volumes

```
G4FieldManager* localFieldMgr = new G4FieldManager(magField);
logVolume->setFieldManager(localFieldMgr, true);
```

where 'true' makes it *push* the field to all the daughter volumes, unless a daughter has its own field manager.
- It is possible to customise the field propagation classes
 - Choosing an appropriate stepper for the field
 - Setting precision parameters

Tunable Parameters

- In addition to the "miss distance" there are two more parameters which can be set in order to adjust the accuracy (and performance) of tracking in a field
 - Such parameters govern the accuracy of the intersection with a volume boundary and the accuracy of the integration of other steps
- The "delta intersection" parameter is the accuracy to which an intersection with a volume boundary is calculated.
 - This parameter is especially important because it is used to limit a bias that the algorithm (for boundary crossing in a field) exhibits
 - The intersection point is always on the 'inside' of the curve. By setting a value for this parameter that is much smaller than some acceptable error, one can limit the effect of this bias



Tunable Parameters

- The “**delta one step**” parameter is the accuracy for the endpoint of 'ordinary' integration steps, those which do not intersect a volume boundary
 - It is a limit on the estimation error of the endpoint of each physics step
- Parameters “**delta intersection**” and “**delta one step**” are strongly coupled
 - These values must be reasonably close to each other (within one order of magnitude)
- Parameters can be set by:

```
theChordFinder->SetDeltaChord ( miss_distance );
```

```
theFieldManager->SetDeltaIntersection ( delta_intersection );
```

```
theFieldManager->SetDeltaOneStep ( delta_one_step );
```

Imprecisions ...

- ... are due to approximating the curved path by linear sections (chords)
 - Parameter to limit this is maximum sagitta δ_{chord}
- ... are due to numerical integration, 'error' in final position and momentum
 - Parameters to limit are $\epsilon_{\text{integration}}$ max, min
- ... are due to intersecting approximate path with the volume boundary
 - Parameter is $\delta_{\text{intersection}}$

Key elements

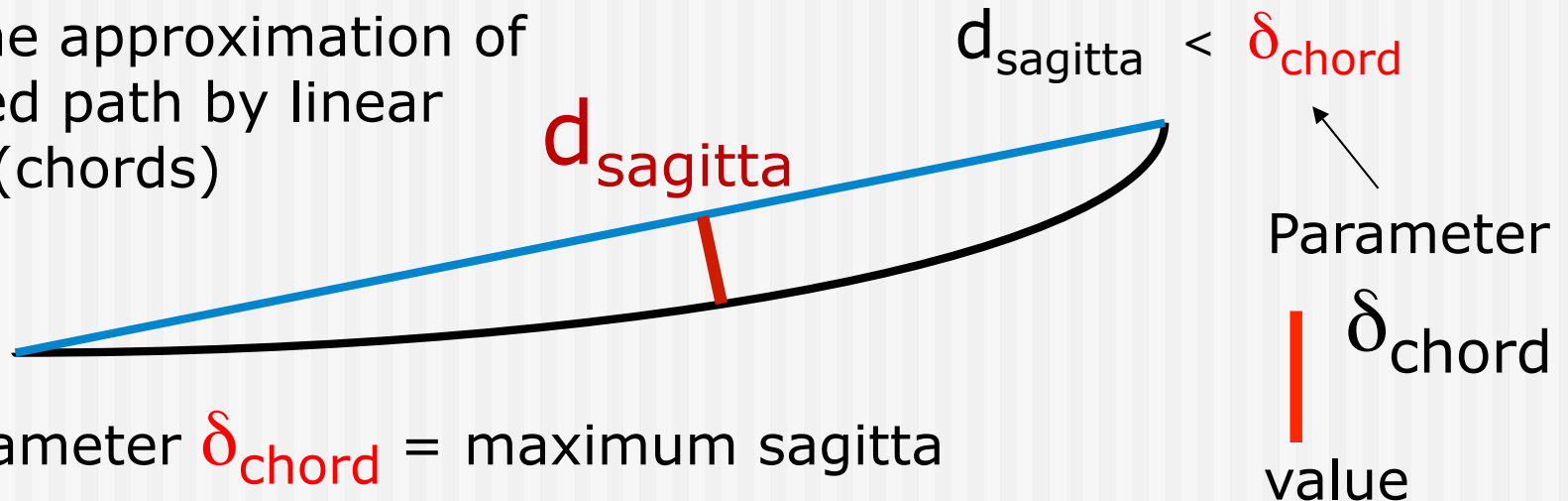
- Precision of track required by the user relates primarily to:
 - The precision (error in position) e_{pos} after a particle has undertaken track length s
 - Precision DE in final energy (momentum) $\delta_E = \Delta E/E$
 - Expected maximum number N_{int} of integration steps
- Recipe for parameters:
 - Set $\epsilon_{integration} (min, max)$ smaller than
 - The minimum ratio of e_{pos} / s along particle's trajectory
 - δ_E / N_{int} the relative error per integration step (in E/p)
 - Choosing how to set δ_{chord} is less well-defined. One possible choice is driven by the typical size of the geometry (size of smallest volume)

Where to find the parameters ...

Parameter	Name	Class	Default value
δ_{miss}	DeltaChord	G4ChordFinder	0.25 mm
d_{min}	stepMinimum	G4ChordFinder	0.01 mm
$\delta_{\text{intersection}}$	DeltaIntersection	G4FieldManager	1 micron
ϵ_{max}	epsilonMax	G4FieldManager	0.001
ϵ_{min}	epsilonMin	G4FieldManager	5 10^{-5}
$\delta_{\text{one step}}$	DeltaOneStep	G4FieldManager	0.01 mm

Volume miss error

- Due to the approximation of the curved path by linear sections (chords)



- Parameter δ_{chord} = maximum sagitta

- Effect of this parameter as $\delta_{\text{chord}} \rightarrow 0$

$$S_{1\text{step}}^{\text{propagator}} \sim (8 \delta_{\text{chord}} R_{\text{curv}})^{1/2}$$

so long as $s^{\text{propagator}} \leftarrow s^{\text{phys}}$ and $s^{\text{propagator}} > d_{\text{min}}(\text{integr})$

Integration error

Due to error in the numerical integration (of equations of motion)

Parameter(s): $\epsilon_{\text{integration}}$

- The size s of the step is limited so that the estimated errors of the final position Δr and momentum Δp are both small enough:

$$\max(\|\Delta r\| / s , \|\Delta p\| / \|p\|) < \epsilon_{\text{integration}}$$

- For Classical RK4 Stepper

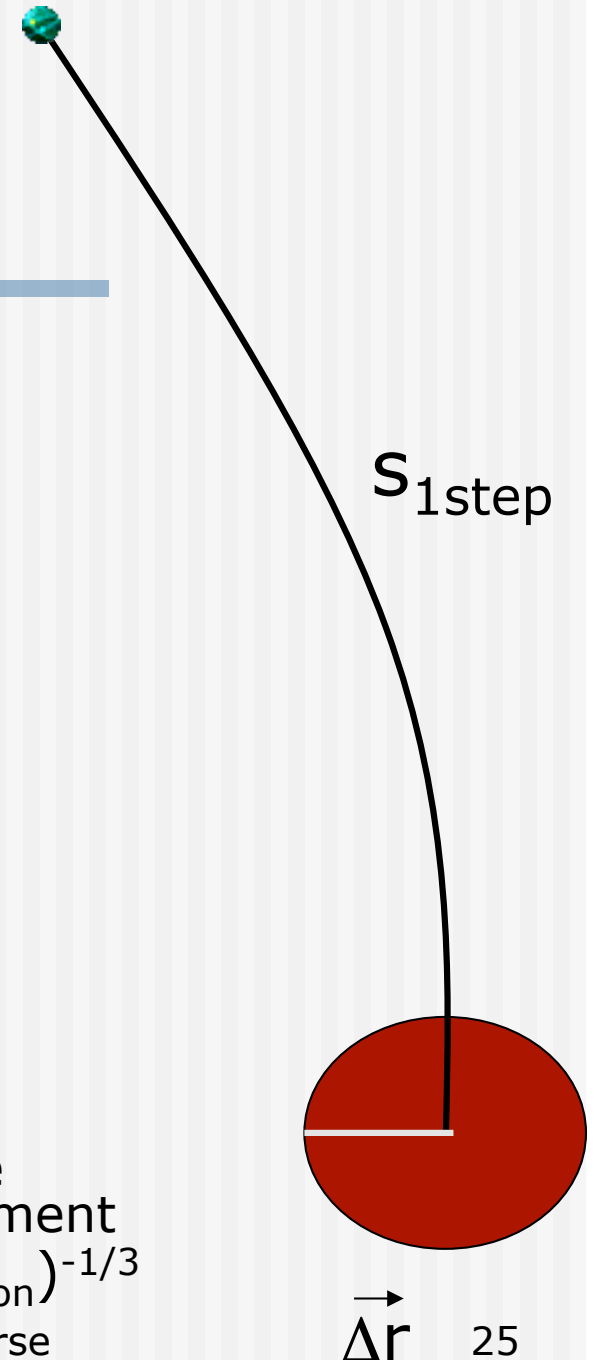
$$s_{\text{1step}}^{\text{integration}} \sim (\epsilon_{\text{integration}})^{1/3}$$

for small enough $\epsilon_{\text{integration}}$

- The integration error should be influenced by the precision of the knowledge of the field (measurement or modeling).

$$N_{\text{steps}} \sim (\epsilon_{\text{integration}})^{-1/3}$$

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Integration error - 2

- $\epsilon_{\text{integration}}$ is currently represented by 3 parameters

- **epsilonMin**, a minimum value (used for big steps)
- **epsilonMax**, a maximum value (used for small steps)
- **DeltaOneStep**, a distance error (for intermediate steps)

Defaults

$0.5 \cdot 10^{-7}$

0.05

0.25 mm

$$\epsilon_{\text{integration}} = \delta_{\text{one step}} / S_{\text{physics}}$$

- Determining a reasonable value

- Suggested to be the minimum of the ratio (accuracy/distance) between sensitive components, ...

- Another parameter

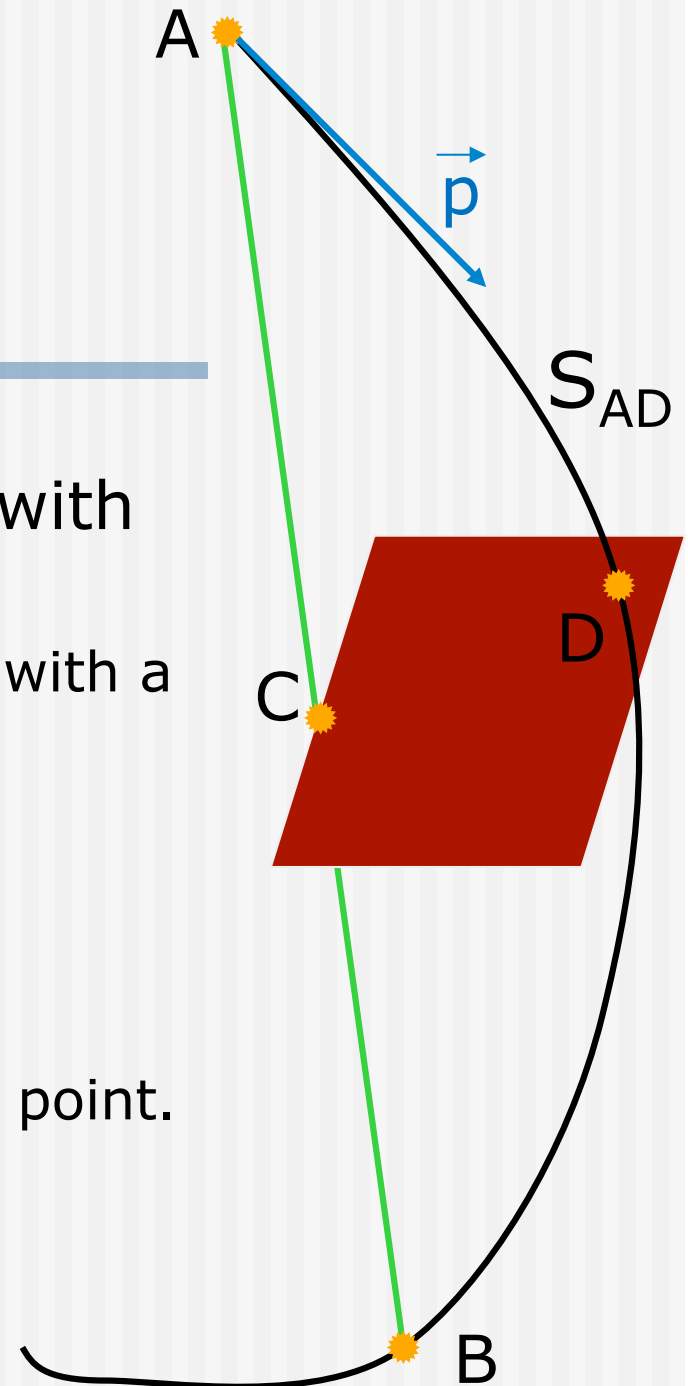
- d_{min} is the minimum step of integration

Default

0.01 mm

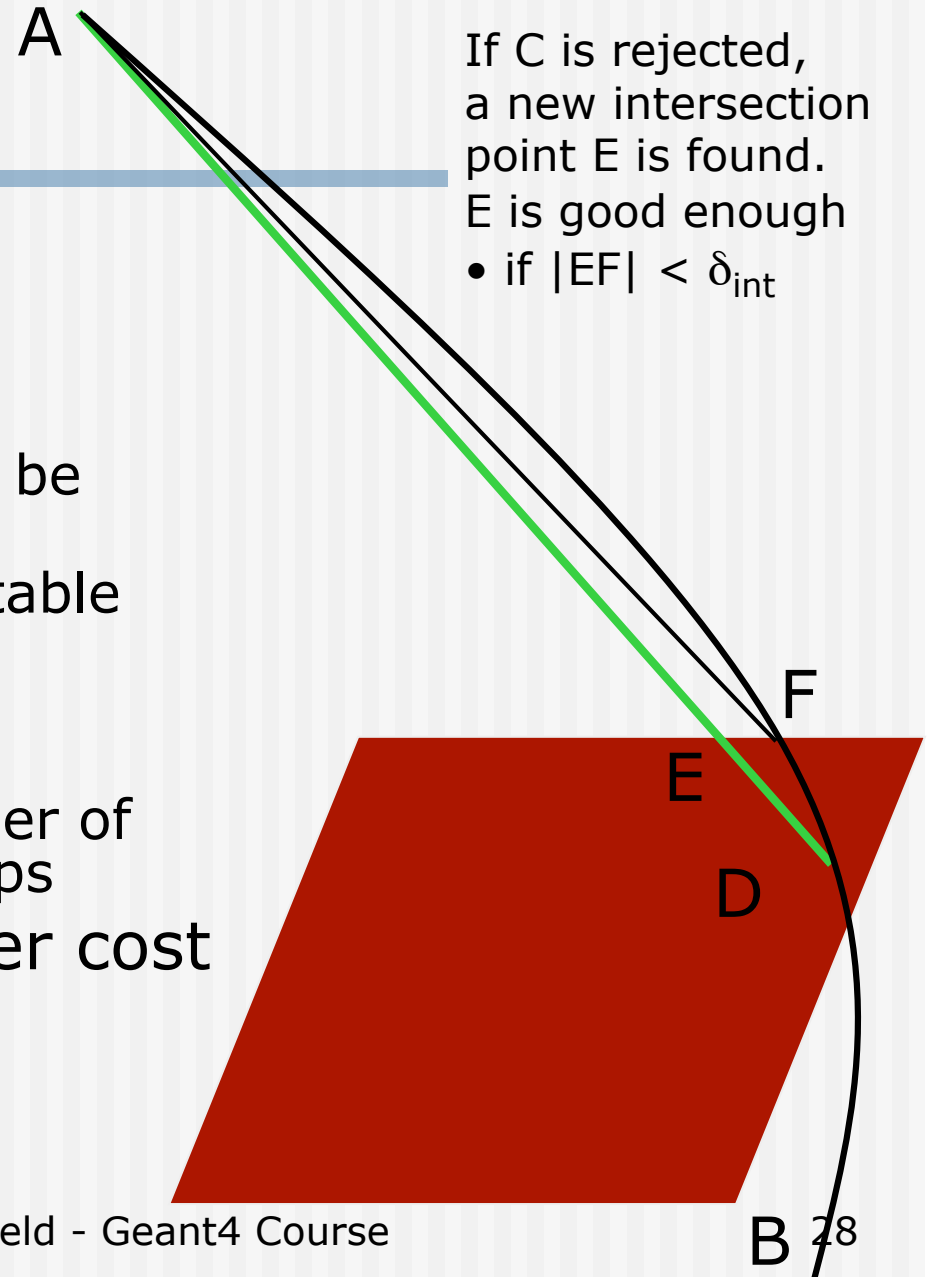
Intersection error

- In intersecting approximate path with volume boundary
 - In trial step AB, intersection is found with a volume at C
 - Step is broken up, choosing D, so
$$S_{AD} = S_{AB} * |AC| / |AB|$$
 - If $|CD| < \delta_{\text{intersection}}$
 - Then C is accepted as intersection point.
 - So δ_{int} is a position error/bias



Intersection error - 2

- δ_{int} must be small
 - compared to tracker hit error
 - its effect on reconstructed momentum estimates should be calculated
 - ... and limited to be acceptable
- Cost of small δ_{int} is less
 - than making δ_{chord} small
 - it is proportional to the number of boundary crossings – not steps
- Quicker convergence / lower cost
 - Possible with optimization



Customizing field integration

- **Runge-Kutta** integration is used to compute the motion of a charged track in a general field. There are many general steppers from which to choose
 - Low and high order, and specialized steppers for pure magnetic fields
- By default, Geant4 uses the classical fourth-order **Runge-Kutta** stepper (**G4ClassicalRK4**), which is general purpose and robust.
 - If the field is known to have specific properties, lower or higher order steppers can be used to obtain the results of same quality using fewer computing cycles
- If the field is calculated from a field map, a lower order stepper is recommended
 - The less smooth the field is, the lower the order of the stepper that should be used
 - The choice of lower order steppers includes the third order stepper (**G4SimpleHeum**) the second order (**G4ImplicitEuler** and **G4SimpleRunge**), and the first order (**G4ExplicitEuler**)
 - A first order stepper would be useful only for very rough fields
 - For somewhat smooth fields (intermediate), the choice between second and third order steppers should be made by trial and error

Customizing field integration

- Trying a few different types of steppers for a particular field or application is suggested if maximum performance is a goal
- Specialized steppers for pure magnetic fields are also available
 - They take into account the fact that a local trajectory in a slowly varying field will not vary significantly from a helix
 - Combining this in with a variation, the Runge-Kutta method can provide higher accuracy at lower computational cost when large steps are possible
- To change the stepper:

theChordFinder

```
->GetIntegrationDriver()
```

```
->RenewStepperAndAdjust( newStepper );
```

Other types of field

- It is possible to create any specialised type of field:
 - inheriting from `G4VField`
 - Associating an *Equation of Motion* class (inheriting from `G4EqRhs`) to simulate other types of fields
 - Fields can be time-dependent
- For pure electric field:
 - `G4ElectricField` and `G4UniformElectricField` classes
- For combined electromagnetic field:
 - `G4ElectroMagneticField` class
- The *Equation of Motion* class for electromagnetic field is `G4MagElectricField`.

```
G4ElectricField* fEMfield
    = new G4UniformElectricField( G4ThreeVector(0., 100000.*kilovolt/cm, 0.) );
G4EqMagElectricField* fEquation = new G4EqMagElectricField(fEMfield);
G4MagIntegratorStepper* fStepper = new G4ClassicalRK4( fEquation, nvar );
G4FieldManager* fFieldMgr
    = G4TransportationManager::GetTransportationManager()->GetFieldManager();
fFieldMgr->SetDetectorField( fEMfield );
G4MagInt_Driver* fIntgrDriver
    = new G4MagInt_Driver(fMinStep, fStepper, fStepper->GetNumberOfVariables() );
G4ChordFinder* fChordFinder = new G4ChordFinder(fIntgrDriver);
```